

Package ‘exdqlm’

September 16, 2026

Title Extended Dynamic Quantile Linear Models

Version 1.1.2

Author Raquel Barata [aut, cre],
Raquel Prado [ths],
Bruno Sanso [ths],
Antonio Aguirre [aut]

Maintainer Raquel Barata <raquel.a.barata@gmail.com>

Description Bayesian quantile-regression routines for dynamic state-space models and static regression under the extended asymmetric Laplace (exAL) error distribution. The dynamic state-space models are extended dynamic quantile linear models (exDQLMs). The package combines dynamic exDQLM inference via Laplace-delta variational Bayes (LDVB), Markov chain Monte Carlo (MCMC), and legacy importance-sampling variational Bayes (ISVB) with static exAL regression via LDVB and MCMC, reduced asymmetric Laplace/dynamic quantile linear model (AL/DQLM) paths through fixed skewness, component builders for trend/seasonality/regression blocks, static shrinkage priors including ridge, regularized horseshoe, and 'rhs_ns', evidence lower bound (ELBO) diagnostics, optional C++ accelerators, and posterior predictive synthesis across separately fitted quantiles through 'quantileSynthesis()'. Dynamic exDQLM methods are described in Barata et al. (2020) <doi:10.1214/21-AOAS1497>.

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Encoding UTF-8

LazyData true

Depends R (>= 3.5)

Imports stats, methods, graphics, coda, tictoc, magic, crch,
truncnorm, LaplacesDemon, grDevices, Rcpp, matrixStats, nimble,
numDeriv

Suggests rmarkdown, testthat (>= 3.0.0), ggplot2, pkgload, MASS

Config/testthat/edition 3

LinkingTo BH, Rcpp, RcppArmadillo, RcppEigen

SystemRequirements C++17; OpenMP (optional)

URL <https://github.com/AntonioAPDL/exdqlm>

BugReports <https://github.com/AntonioAPDL/exdqlm/issues>

Config/roxygen2/version 8.0.0

NeedsCompilation yes

Repository CRAN

Date/Publication 2026-09-16 01:00:02 UTC

Contents

exdqlm-package	4
+exdqlm	7
as.exdqlm	8
BTflow	8
climateIndices	9
compPlot	10
dexal	11
diagnostics	12
diagnostics.exalStaticFit	13
diagnostics.exdqlmFit	14
diagnostics.exdqlmForecast	17
ELIanom	19
exalStaticDiagnostics	19
exalStaticLDVB	21
exalStaticMCMC	25
exal_make_mcmc_control	30
exal_make_mcmc_dqlm_sigma_control	31
exal_make_mcmc_latent_state_control	31
exal_make_mcmc_sigmagam_control	32
exal_make_mcmc_theta_control	33
exal_make_vb_control	34
exal_make_vb_sigmagam_control	35
exal_make_vb_sts_control	36
exdqlmDiagnostics	37
exdqlmForecast	39
exdqlmForecastDiagnostics	41
exdqlmISVB	43
exdqlmLDVB	46
exdqlmMCMC	49
exdqlmPlot	53
exdqlmTransferISVB	55
exdqlmTransferLDVB	58
exdqlmTransferMCMC	62
get_gamma_bounds	67
is.exalStaticDiagnostic	68
is.exalStaticFit	68
is.exalStaticLDVB	68

is.exalStaticMCMC	69
is.exdqlm	69
is.exdqlmDiagnostic	69
is.exdqlmFit	70
is.exdqlmForecast	70
is.exdqlmForecastDiagnostic	70
is.exdqlmISVB	71
is.exdqlmLDVB	71
is.exdqlmMCMC	71
is.exdqlmSynthesis	72
pexal	72
plot.exalStaticDiagnostic	73
plot.exalStaticFit	74
plot.exalStaticLDVB	75
plot.exalStaticMCMC	75
plot.exdqlmDiagnostic	76
plot.exdqlmFit	77
plot.exdqlmForecast	79
plot.exdqlmISVB	79
plot.exdqlmLDVB	80
plot.exdqlmMCMC	81
plot.exdqlmSynthesis	82
polytrendMod	83
predict.exdqlmFit	84
print.exalStaticDiagnostic	86
print.exalStaticFit	86
print.exalStaticLDVB	87
print.exalStaticMCMC	87
print.exdqlm	88
print.exdqlmDiagnostic	88
print.exdqlmFit	89
print.exdqlmForecast	89
print.exdqlmForecastDiagnostic	90
print.exdqlmISVB	90
print.exdqlmLDVB	91
print.exdqlmMCMC	92
print.exdqlmSynthesis	92
qexal	93
quantileSynthesis	94
regMod	96
rexal	97
scIVTmag	98
seasMod	98
summary.exalStaticDiagnostic	99
summary.exalStaticFit	99
summary.exalStaticLDVB	100
summary.exalStaticMCMC	100
summary.exdqlm	101

summary.exdqlmDiagnostic	101
summary.exdqlmFit	102
summary.exdqlmForecast	102
summary.exdqlmForecastDiagnostic	103
summary.exdqlmISVB	103
summary.exdqlmLDVB	104
summary.exdqlmMCMC	105
summary.exdqlmSynthesis	105

Index	107
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exdqlm-package	<i>exdqlm: Extended Dynamic Quantile Linear Models</i>
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Description

Bayesian quantile-regression tools for dynamic state-space models and static regression under the extended asymmetric Laplace error distribution (exAL).

Details

The package centers on native dynamic quantile state-space modeling for univariate time series and also provides a static exAL regression workflow. Across these settings, exdqlm combines model construction helpers, multiple Bayesian inference engines, shrinkage priors for static coefficients, and post hoc synthesis of several fitted quantiles.

Main workflows

- Dynamic/state-space quantile modeling via `exdqlmLDVB()` and `exdqlmMCMC()`, with legacy `exdqlmISVB()` retained for backward compatibility and transfer-function extensions through `exdqlmTransferLDVB()`, `exdqlmTransferMCMC()`, and legacy `exdqlmTransferISVB()`. Dynamic fitted objects support standard `plot()`, `predict()`, and `diagnostics()` methods, with `exdqlmPlot()`, `compPlot()`, `exdqlmForecast()`, and the named diagnostic helpers retained as explicit helpers.
- Static Bayesian exAL regression via `exalStaticLDVB()` and `exalStaticMCMC()`, with fitted-quantile plots through `plot()` and static diagnostics through `diagnostics()`.
- Modular state-space construction via `polytrendMod()`, `seasMod()`, and `regMod()`.
- Multi-quantile post-processing via `quantileSynthesis()` for post hoc posterior-predictive synthesis from separately fitted quantiles into a unified predictive distribution.

Object system

- Model specifications have class `exdqlm` and can be combined with the `+` method.
- Dynamic fitted objects keep their engine-specific first class (`exdqlmLDVB`, `exdqlmMCMC`, or legacy `exdqlmISVB`) and also inherit from the shared `exdqlmFit` family. They support `print()`, `summary()`, `plot()`, and `predict()` where natural.

- Static fitted objects keep their engine-specific first class (`exalStaticLDVB` or `exalStaticMCMC`) and also inherit from the shared `exalStaticFit` family. They support `print()`, `summary()`, fitted-quantile `plot()`, and `diagnostics()` methods.
- Post-processing functions return explicit objects: `exdqlmDiagnostic`, `exdqlmForecast`, `exdqlmForecastDiagnostic`, `exdqlmSynthesis`, and `exalStaticDiagnostic`. These objects can be inspected with standard `print()/summary()` methods and plotted with `plot()` when a display is defined.

Distinctive features

- Dynamic Bayesian quantile state-space inference with structured Laplace-delta variational Bayes (LDVB) as the main variational Bayes (VB) engine, Markov chain Monte Carlo (MCMC) for posterior simulation, and legacy importance-sampling variational Bayes (ISVB) retained for compatibility and historical comparisons.
- A unified package covering both dynamic exDQLM models and static exAL regression.
- Static shrinkage priors including ridge, regularized horseshoe ("`rhs`"), and `rhs_ns`.
- Reduced AL/DQLM paths through `dqlm.ind = TRUE` in both dynamic and static APIs.
- Standardized VB diagnostics traces via `fit$diagnostics$vb_trace` for the evidence lower bound (ELBO), `sigma`, `gamma`, and convergence deltas across VB engines.
- Conservative automatic warmup defaults for the most failure-prone shared blocks: RHS-family tau scheduling plus exAL (`sigma`, `gamma`) warmup in VB and MCMC entry points, with explicit controls available only when users need to override the defaults.
- Structured exAL scale-skewness updates: unrestricted exAL LDVB fits use a $q(\gamma) \mid q(\sigma \mid \gamma)$ block by default, and unrestricted exAL MCMC fits use an exact scale-collapsed gamma slice transition by default.
- Optional C++ acceleration for selected state-space computations.

Release changes in 1.1.2

- The fast C++ dynamic MCMC FFBS backend now uses a Cholesky covariance square root for stochastic state simulation. This avoids platform-dependent SVD bases in fixed-seed multivariate-normal state draws while preserving the same Gaussian smoothing target.

Release changes in 1.1.1

- Stochastic compiled helper paths were made serial and controlled by the R random-number generator, improving exact repeatability under fixed seeds.
- The default unrestricted exAL MCMC kernel changed to `mh.proposal = "collapsed_slice"`, which integrates out `sigma` for the `gamma` slice step and then redraws `sigma` from its exact GIG conditional. Legacy kernels remain available when selected explicitly.
- The default unrestricted exAL LDVB scale-skewness factor changed to a structured $q(\gamma) \mid q(\sigma \mid \gamma)$ approximation. The previous two-dimensional Laplace-delta factor remains available through `exal_make_vb_sigmagam_control(factorization = "laplace_delta")`.

Release changes in 1.1.0

- Shared fit class families were added while preserving the existing first-class object names: dynamic fits inherit from `exdqlmFit`, and static fits inherit from `exalStaticFit`.
- Fitted-model and post-processing objects have standardized `print()` and `summary()` methods for inspecting object type, engine, dimensions, stored draws, diagnostics, and run time.
- Dynamic fits support standard `plot()`, `predict()`, and `diagnostics()` methods; forecast and static-fit diagnostics use the same `diagnostics()` generic where defined.

Release changes in 1.0.0

- Dynamic diagnostics report CRPS through a finite integrated quantile-score approximation over posterior predictive empirical quantiles, with user-configurable quantile levels and weights in `exdqlmDiagnostics()`.
- Held-out forecast diagnostics are available for forecast objects through `diagnostics()`.
- Static diagnostics store fitted-quantile summaries and coefficient intervals, with `plot(..., type = "coefficients")` available for comparing static LDVB and MCMC coefficient summaries.
- Dynamic KL normality diagnostics are deterministic for fixed fitted objects and no longer depend on stochastic reference samples. The top-level diagnostic object exposes KL as the primary calibration diagnostic and keeps advanced KL sensitivity details under `kl.details`.

Runtime options

- `options(exdqlm.use_cpp_kf = TRUE|FALSE)` – C++ Kalman bridge (optional; default TRUE).
- `options(exdqlm.compute_elbo = TRUE|FALSE)` – Compute ELBO (optional; default TRUE).
- `options(exdqlm.tol_elbo = numeric)` – Positive ELBO convergence tolerance used when `exdqlm.compute_elbo = TRUE`; smaller values enforce stricter ELBO stabilization checks (default $1e-6$).
- `options(exdqlm.use_cpp_builders = TRUE|FALSE)` – C++ model builders (optional; default FALSE).
- `options(exdqlm.use_cpp_samplers = TRUE|FALSE)` – C++ samplers (optional; default FALSE).
- `options(exdqlm.use_cpp_postpred = TRUE|FALSE)` – C++ posterior predictive sampler (optional; default FALSE).
- `options(exdqlm.use_cpp_mcmc = TRUE|FALSE)` – MCMC backend routing (optional; default TRUE).
- `options(exdqlm.cpp_mcmc_mode = "strict"|"fast")` – strict keeps legacy R-kernel parity; fast enables C++ FFBS in MCMC (default "fast"). In version 1.1.2 and later, fast-mode stochastic state draws use a Cholesky covariance square root for fixed-seed platform stability.
- `options(exdqlm.cpp_threads = numeric)` – Reserved compatibility option for eligible compiled paths. Stochastic compiled samplers use serial R-controlled RNG streams in version 1.1.1 and later.

Author(s)

Maintainer: Raquel Barata <raquel.a.barata@gmail.com>

Authors:

- Raquel Barata <raquel.a.barata@gmail.com>
- Antonio Aguirre

Other contributors:

- Raquel Prado [thesis advisor]
- Bruno Sanso [thesis advisor]

See Also

Useful links:

- <https://github.com/AntonioAPDL/exdqlm>
- Report bugs at <https://github.com/AntonioAPDL/exdqlm/issues>

+.exdqlm

Addition for exdqlm objects

Description

Combines two state space blocks into a single state space model for an exDQLM.

Usage

```
## S3 method for class 'exdqlm'
m1 + m2
```

Arguments

m1	object of class "exdqlm" containing the first model to be combined.
m2	object of class "exdqlm" containing the second model to be combined.

Value

An object of class "exdqlm" containing the new combined state space model components:

- FF - Observational vector.
- GG - Evolution matrix.
- m0 - Prior mean of the state vector.
- C0 - Prior covariance of the state vector.

Examples

```
trend.comp = polytrendMod(2, rep(0, 2), 10*diag(2))
seas.comp = seasMod(365, c(1,2,4), C0 = 10*diag(6))
model = trend.comp + seas.comp
```

as.exdqlm	exdqlm <i>objects</i>
-----------	-----------------------

Description

as.exdqlm attempts to turn a list into an exdqlm object. Works for time-invariant dlm objects created using the **dlm** package.

Usage

```
as.exdqlm(m)
```

Arguments

m a list containing named elements m0, C0, FF and GG.

Value

An object of class "exdqlm" containing the state space model components:

- FF - Observational vector.
- GG - Evolution matrix.
- m0 - Prior mean of the state vector.
- C0 - Prior covariance of the state vector.

BTflow	<i>Monthly streamflow at the Big Trees gauge</i>
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Description

Observed monthly mean streamflow, in cubic feet per second, at the Big Trees gauge on the San Lorenzo River in Santa Cruz County, California. The monthly values were obtained by averaging the daily USGS streamflow observations within each calendar month.

Usage

```
BTflow
```

Format

A monthly time series (ts) of length 471, spanning January 1987 through March 2026.

Source

U.S. Geological Survey, National Water Information System (USGS Water Data for the Nation), <https://waterdata.usgs.gov/>.

References

U.S. Geological Survey (2016). National Water Information System data available on the World Wide Web (USGS Water Data for the Nation). <https://waterdata.usgs.gov/>.

climateIndices

Monthly climate indices for streamflow examples

Description

Monthly atmospheric and oceanic climate indices used as external predictors in the Big Trees streamflow examples. Values are stored on their original scales; examples that combine indices standardize the relevant columns within the analysis code.

Usage

climateIndices

Format

A data frame with 516 rows and 3 variables:

date First day of the calendar month.

noi Northern Oscillation Index.

amo Atlantic Multidecadal Oscillation index.

The data frame spans January 1980 through December 2022.

Source

Compiled from the NOAA Physical Sciences Laboratory monthly climate indices collection, <https://psl.noaa.gov/data/climateindices/>.

compPlot

*Plot a component of an exDQLM***Description**

The function plots posterior mean summaries and 95% credible intervals (CrIs) of a specified component of an exDQLM. Alternatively, if `just.theta=TRUE`, posterior mean summaries and 95% CrIs of a single element of the dynamic state vector are plotted.

Usage

```
compPlot(
  m1,
  index,
  add = FALSE,
  col = "purple",
  just.theta = FALSE,
  cr.percent = 0.95,
  plot = TRUE,
  xlim = NULL,
  ylim = NULL,
  xlab = "time",
  ylab = NULL,
  lwd = 1.5,
  lwd.interval = 0.75,
  lty.interval = 2
)
```

Arguments

<code>m1</code>	A fitted dynamic <code>exdqlmFit</code> object, such as an object returned by <code>exdqlmLDVB</code> , <code>exdqlmMCMC</code> , or legacy <code>exdqlmISVB</code> .
<code>index</code>	Vector of consecutive integers in $\{1, \dots, q\}$ indicating the component or element of the state vector to be plotted.
<code>add</code>	Logical value indicating whether the dynamic component will be added to existing plot. Default is <code>FALSE</code> .
<code>col</code>	Character vector of length 1 giving color of the dynamic component to be plotted. Default is <code>purple</code> .
<code>just.theta</code>	Logical; if <code>TRUE</code> , the function plots the dynamic distribution of the index element of the state vector. If <code>just.theta=TRUE</code> , <code>index</code> must have length 1.
<code>cr.percent</code>	Numeric in $(0, 1)$ indicating the probability mass for the credible intervals (e.g., 0.95). Default 0.95.
<code>plot</code>	Logical value indicating whether to draw the plot. If <code>FALSE</code> , the function only returns the plotted summaries. Default is <code>TRUE</code> .
<code>xlim, ylim</code>	Optional limits passed to the base plotting call when <code>plot = TRUE</code> .

<code>xlab, ylab</code>	Optional axis labels passed to the base plotting call when <code>plot = TRUE</code> .
<code>lwd, lwd.interval</code>	Line widths for the dynamic component and credible interval bounds, respectively.
<code>lty.interval</code>	Line type for the credible interval bounds.

Value

A list of the following is returned:

- `map.comp` - Posterior mean summary of the dynamic component (or element of the state vector; legacy field name retained for backward compatibility).
- `lb.comp` - Lower bound of the 95% CrIs of the dynamic component (or element of the state vector).
- `ub.comp` - Upper bound of the 95% CrIs of the dynamic component (or element of the state vector).
- `x` - Time/index values used for plotting.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:80]
trend.comp = polytrendMod(2, rep(0, 2), 10*diag(2))
seas.comp = seasMod(365, c(1, 2), C0 = 10*diag(4))
model = trend.comp + seas.comp
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.98, 1), dim.df = c(2, 4),
               gam.init = -3.5, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
# plot first harmonic component
compPlot(M0, index = c(3, 4), col = "blue")
c.summary = compPlot(M0, index = c(3, 4), plot = FALSE)
options(old)
```

dexal	<i>Density Function for the Extended Asymmetric Laplace (exAL) Distribution</i>
-------	---

Description

Computes the PDF of the Extended Asymmetric Laplace (exAL) distribution. Vectorized over `x`.

Usage

```
dexal(x, p0 = 0.5, mu = 0, sigma = 1, gamma = 0, log = FALSE)
```

Arguments

<code>x</code>	Numeric vector of quantiles.
<code>p0</code>	Probability level used in the quantile parametrization. Scalar in (0, 1). Default 0.5.
<code>mu</code>	Location parameter (scalar). Default 0.
<code>sigma</code>	Scale parameter (scalar, strictly positive). Default 1.
<code>gamma</code>	Skewness parameter controlling asymmetry (scalar). Must be within valid bounds implied by <code>p0</code> . Default 0.
<code>log</code>	Logical scalar; if TRUE return log-density. Default FALSE.

Value

Numeric vector of densities (same length as `x`).

Examples

```
dexal(0)
dexal(1, p0 = 0.75, mu = 0, sigma = 2, gamma = 0.25)
dexal(seq(-3, 3, by = 0.1), p0 = 0.3, mu = 0, sigma = 1, gamma = -0.45)
```

diagnostics

Diagnostics Generic

Description

Compute diagnostic summaries for fitted and post-processing objects.

Usage

```
diagnostics(object, ...)
```

Arguments

<code>object</code>	An object of class <code>exdqlmFit</code> , <code>exdqlmForecast</code> , or <code>exalStaticFit</code> .
<code>...</code>	Additional arguments passed to specific methods.

Details

`diagnostics()` is the standard diagnostic entry point for the main fitted-object families in **exdqlm**. Methods are currently provided for dynamic fitted models, dynamic forecast objects, and static AL/exAL fitted models. The returned objects can be inspected with `print()` or `summary()`, and plotted with `plot()` when a diagnostic display is defined.

Value

The output depends on the method: `diagnostics.exdqlmFit()` returns an `exdqlmDiagnostic` object, `diagnostics.exdqlmForecast()` returns an `exdqlmForecastDiagnostic` object, and `diagnostics.exalStaticFit` returns an `exalStaticDiagnostic` object.

`diagnostics.exalStaticFit`

Diagnostics Method for exalStaticFit Objects

Description

Diagnostics for a fitted static quantile model. The function summarizes fitted quantiles on a shared design matrix, reports mean check loss against observed responses when available, and can optionally compare the fitted quantile curve against a known reference quantile function. The returned diagnostic object also stores posterior summaries for the static regression coefficients, which can be plotted with `plot(..., type = "coefficients")`.

Usage

```
## S3 method for class 'exalStaticFit'
diagnostics(
  object,
  m2 = NULL,
  X = NULL,
  y = NULL,
  ref = NULL,
  plot = FALSE,
  cols = c("red", "blue"),
  cr.percent = 0.95,
  ...
)
```

Arguments

<code>object</code>	A fitted static <code>exalStaticFit</code> object.
<code>m2</code>	Optional second fitted static <code>exalStaticFit</code> object to compare against <code>object</code> .
<code>X</code>	Optional design matrix. If omitted, the function uses <code>object\$X</code> when available.
<code>y</code>	Optional response vector. If omitted, the function uses <code>object\$y</code> when available.
<code>ref</code>	Optional reference quantile vector on the same rows as <code>X</code> .
<code>plot</code>	Logical; if TRUE, immediately plot the returned static-diagnostic object as a convenience shortcut. Default is FALSE; the preferred workflow is to save the object and then call <code>plot()</code> on it.
<code>cols</code>	Character vector of length 1 or 2 giving colors for plotted diagnostics.
<code>cr.percent</code>	Credible-interval mass used when summarizing fitted quantiles.
<code>...</code>	Additional arguments (unused).

Details

`exalStaticDiagnostics()` is designed for the static regression setting. It reports fitted quantile summaries on a common design matrix, optional mean check loss against observed responses, optional reference-curve errors, coefficient posterior summaries, and compact comparison plots. The returned object can be printed, summarized, or plotted with standard methods. The `ref` argument is a reference conditional quantile evaluated on the rows of `X`; it is distinct from the optional `beta.ref` argument of `plot.exalStaticDiagnostic`, which is used only to overlay known coefficient values in simulation examples.

Value

An object of class "exalStaticDiagnostic" containing fitted-quantile summaries, residual summaries (when `y` is provided), optional reference-curve error metrics, coefficient posterior summaries, and run-time metadata for object and `m2` (if supplied).

Examples

```
set.seed(1)
x <- seq(-2, 2, length.out = 60)
X <- cbind(1, x)
y <- 0.5 * x + (1.2 + 0.35 * x) * stats::rnorm(length(x))
q_true <- 0.5 * x + (1.2 + 0.35 * x) * stats::qnorm(0.25)

fit_ldvb <- exalStaticLDVB(
  y = y, X = X, p0 = 0.25,
  max_iter = 60, tol = 1e-3,
  verbose = FALSE
)
fit_mcmc <- exalStaticMCMC(
  y = y, X = X, p0 = 0.25,
  n.burn = 60, n.mcmc = 60,
  verbose = FALSE
)
out <- diagnostics(fit_ldvb, fit_mcmc, ref = q_true)
plot(out)
plot(out, type = "coefficients")
```

diagnostics.exdqlmFit *Diagnostics Method for Dynamic exdqlmFit Objects*

Description

Diagnostics for a fitted dynamic quantile model. The function computes the following for the model(s) provided: the posterior predictive loss criterion based off the check loss, the CRPS approximated as a finite integrated quantile score over posterior predictive empirical quantiles, the one-step-ahead distribution sequence, and deterministic semiclosed KL normality diagnostics for

the MAP standardized forecast errors. The returned diagnostic object can be printed, summarized, or plotted with standard methods. Calling `plot()` on the object produces the QQ plot and ACF plot corresponding to the one-step-ahead distribution sequence, together with a time series plot of the MAP standard forecast errors.

Usage

```
## S3 method for class 'exdqlmFit'
diagnostics(
  object,
  m2 = NULL,
  plot = FALSE,
  cols = c("red", "blue"),
  ref = NULL,
  crps_probs = seq(0.01, 0.99, by = 0.01),
  crps_weights = NULL,
  kl_k = NULL,
  ...
)
```

Arguments

<code>object</code>	A fitted dynamic <code>exdqlmFit</code> object.
<code>m2</code>	An optional second fitted dynamic <code>exdqlmFit</code> object to compare with <code>object</code> .
<code>plot</code>	Logical value indicating whether to immediately plot the returned diagnostic object as a convenience shortcut. Default is <code>FALSE</code> ; the preferred workflow is to save the object and then call <code>plot()</code> on it.
<code>cols</code>	Character vector of length 1 or 2 giving color(s) used to plot diagnostics. Default <code>c("red", "blue")</code> .
<code>ref</code>	Optional finite reference sample of size <code>length(object\$y)</code> from a standard normal distribution. Used for the reversed KL diagnostic. When <code>NULL</code> , a deterministic standard-normal quantile grid is used.
<code>crps_probs</code>	Numeric vector of quantile levels used to approximate CRPS through the integrated quantile-score identity. Values must be strictly between 0 and 1. Default is <code>seq(0.01, 0.99, by = 0.01)</code> .
<code>crps_weights</code>	Optional non-negative numeric weights for <code>crps_probs</code> . When <code>NULL</code> , equal weights are used. When provided, weights are normalized to sum to 1.
<code>kl_k</code>	Optional positive integer vector of nearest-neighbor values used for the KL entropy and cross-entropy estimates. When <code>NULL</code> , the default grid <code>c(3, 5, 10, 20, 30)</code> is filtered to values supported by the finite standardized-error sample size, falling back to 1 for very small samples.
<code>...</code>	Additional arguments (unused).

Details

The primary KL summary is computed from the MAP standardized one-step-ahead forecast errors `map.standard.forecast.errors`. The reported KL value is the user-facing calibration diagnostic

and estimates $KL(P_e || N(0, 1))$, where P_e is the continuous diagnostic-error law represented by the standardized errors. It uses the semiclosed identity $KL(P_e || N(0, 1)) = CE(P_e, N(0, 1)) - H(P_e)$, with the normal cross-entropy term evaluated analytically and the entropy estimated by a one-dimensional k-nearest-neighbor estimator. The reported `KL.flip` estimates the reversed diagnostic $KL(N(0, 1) || P_e)$ using kNN cross-entropy. The reversed direction is more sensitive and should be read as a secondary sensitivity diagnostic, not as a replacement for KL. Advanced by-k sensitivity tables and Gaussian plug-in checks are stored under `kl.details` so the top-level diagnostic object exposes a single primary KL value. Negative finite-sample estimates are not clamped; they indicate estimator bias or instability for the current sample.

Value

An object of class "exdqlmDiagnostic" containing the following:

- `m1.uts` - The one-step-ahead distribution sequence of object.
- `m1.KL` - The forward KL normality diagnostic $KL(P_{\text{error}} || N(0, 1))$ for the MAP standardized forecast errors.
- `m1.KL.flip` - The reversed ("flipped") KL diagnostic $KL(N(0, 1) || P_{\text{error}})$ for the MAP standardized forecast errors; this is a secondary sensitivity diagnostic.
- `m1.CRPS` - The mean CRPS approximated by a finite integrated quantile score over posterior predictive empirical quantiles.
- `m1.pplc` - The posterior predictive loss criterion of object based off the check loss function.
- `m1.qq` - The ordered pairs of the qq-plot comparing `m1.uts` with a standard normal distribution.
- `m1.acf` - The autocorrelations of `m1.uts` by lag.
- `m1.rt` - Run-time of the original model `m1` in seconds.
- `m1.msfe` - MAP standardized one-step-ahead forecast errors from the original model `m1`.
- `y` - The original time-series used to fit object.
- `crps.method` - The CRPS approximation method.
- `crps.probs` - The quantile levels used for the CRPS approximation.
- `crps.weights` - The normalized weights used for the CRPS approximation.
- `kl.method`, `kl.k`, `kl.aggregate`, and `kl.reference` - KL estimator metadata.
- `kl.n_finite`, `kl.n_ref`, and `kl.zero_distance_count` - KL diagnostic sample-size and distance-floor metadata.
- `kl.details` - Advanced KL estimator details by model. For each model this includes primary/flipped definitions, by-k sensitivity tables, a Gaussian plug-in check, and estimator metadata.

If `m2` is provided, analogous results for `m2` are also included in the list.

An object of class `exdqlmDiagnostic`.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.95), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
M0.diags = diagnostics(M0)
M0.diags
plot(M0.diags)
options(old)
```

diagnostics.exdqlmForecast

Diagnostics Method for exdqlmForecast Objects

Description

Computes held-out forecast scores from one or two `exdqlmForecast` objects, typically returned by `predict.exdqlmFit` or `exdqlmForecast` with `return.draws = TRUE`. This method evaluates posterior predictive forecast draws against observations reserved outside the fitted sample.

Usage

```
## S3 method for class 'exdqlmForecast'
diagnostics(
  object,
  y,
  m2 = NULL,
  p0 = NULL,
  crps_probs = seq(0.01, 0.99, by = 0.01),
  crps_weights = NULL,
  ...
)
```

Arguments

<code>object</code>	An <code>exdqlmForecast</code> object returned by <code>predict.exdqlmFit</code> or <code>exdqlmForecast</code> with <code>return.draws = TRUE</code> .
<code>y</code>	Required numeric vector or time series of held-out observations. Its length must equal the forecast horizon.
<code>m2</code>	An optional second object of class "exdqlmForecast" to compare with <code>object</code> .

<code>p0</code>	Optional quantile level used for the check-loss calculation. When NULL, the value is taken from <code>object\$m1\$p0</code> . If <code>m2</code> is supplied, its fitted quantile level must agree with the resolved value.
<code>crps_probs</code>	Optional numeric vector of quantile levels used to approximate CRPS through the integrated quantile-score identity. Values must be strictly between 0 and 1. Default is <code>seq(0.01, 0.99, by = 0.01)</code> .
<code>crps_weights</code>	Optional non-negative numeric weights for <code>crps_probs</code> . When NULL, equal weights are used. When provided, weights are normalized to sum to 1.
<code>...</code>	Additional arguments (unused).

Details

The check loss is computed at the target quantile level `p0` using the forecast quantile means `ff` stored in each forecast object. CRPS is computed from `samp.fore` using the same finite integrated quantile-score approximation used by `exdqlmDiagnostics()`. This function does not compute KL diagnostics because KL in **exdqlm** is defined for fitted one-step-ahead MAP standardized forecast errors, not for arbitrary held-out forecast draws.

Value

An object of class "exdqlmForecastDiagnostic" containing:

- `y` - Held-out observations used for scoring.
- `p0` - Quantile level used for check loss.
- `horizon` - Forecast horizon.
- `m1.check_loss` - Mean target-quantile check loss for `m1`.
- `m1.CRPS` - Mean CRPS approximation for `m1`.
- `m1.pointwise` - Pointwise held-out scores for `m1`.
- `crps.method`, `crps.probs`, and `crps.weights` - CRPS approximation metadata.

If `m2` is supplied, analogous `m2.*` fields are included.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:65]
y_train = y[1:60]
y_holdout = y[61:65]
model = polytrendMod(1, stats::quantile(y_train, 0.85), 10)
M0 = exdqlmLTVB(y_train, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               dqlm.ind = TRUE, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
fFF = model$FF[, 1, drop = FALSE]
fGG = model$GG
M0.forecast = predict(M0, start.t = 60, k = 5,
                     fFF = fFF, fGG = fGG,
                     return.draws = TRUE, n.samp = 20, seed = 123,
```

```

                                plot = FALSE)
score = diagnostics(M0.forecast, y = y_holdout)
score

```

ELIanoms

Daily time-series of ELI anomalies.

Description

ELI anomalies on the daily time-scale from January 1, 1979 to December 31, 2019 with all February 29ths omitted.

Usage

ELIanoms

Format

A time series of length 14965.

Source

<https://portal.nersc.gov/archive/home/projects/cascade/www/ELI>

References

Patricola, C.M., O'Brien, J.P., Risser, M.D. et al. *Maximizing ENSO as a source of western US hydroclimate predictability*. *Clim Dyn* 54, 351–372 (2020). doi:10.1007/s00382019050048

exalStaticDiagnostics *exAL Diagnostics*

Description

Static diagnostics companion for `exalStaticLDVB()` and `exalStaticMCMC()`. The function summarizes fitted quantiles on a shared design matrix, reports mean check loss against observed responses when available, and can optionally compare the fitted quantile curve against a known reference quantile function. The returned diagnostic object also stores posterior summaries for the static regression coefficients, which can be plotted with `plot(..., type = "coefficients")`.

Usage

```
exalStaticDiagnostics(
  m1,
  m2 = NULL,
  X = NULL,
  y = NULL,
  ref = NULL,
  plot = FALSE,
  cols = c("red", "blue"),
  cr.percent = 0.95
)
```

Arguments

m1	A fitted static <code>exalStaticFit</code> object, such as an object returned by exalStaticLDVB or exalStaticMCMC .
m2	Optional second fitted static <code>exalStaticFit</code> object to compare against m1.
X	Optional design matrix. If omitted, the function uses <code>m1\$X</code> when available.
y	Optional response vector. If omitted, the function uses <code>m1\$y</code> when available.
ref	Optional reference quantile vector on the same rows as X.
plot	Logical; if TRUE, immediately plot the returned static-diagnostic object as a convenience shortcut. Default is FALSE; the preferred workflow is to save the object and then call <code>plot()</code> on it.
cols	Character vector of length 1 or 2 giving colors for plotted diagnostics.
cr.percent	Credible-interval mass used when summarizing fitted quantiles.

Details

Unlike [exdqlmDiagnostics](#), which is built around one-step-ahead dynamic forecast diagnostics, `exalStaticDiagnostics()` is designed for the static regression setting. It reports fitted quantile summaries on a common design matrix, optional mean check loss against observed responses, optional reference-curve errors, coefficient posterior summaries, and compact comparison plots. The returned object can be printed, summarized, or plotted with standard methods. The `ref` argument is a reference conditional quantile evaluated on the rows of X; it is distinct from the optional `beta.ref` argument of [plot.exalStaticDiagnostic](#), which is used only to overlay known coefficient values in simulation examples.

Value

An object of class `"exalStaticDiagnostic"` containing fitted-quantile summaries, residual summaries (when `y` is provided), optional reference-curve error metrics, coefficient posterior summaries, and run-time metadata for `m1` and `m2` (if supplied).

Examples

```
set.seed(1)
x <- seq(-2, 2, length.out = 60)
```

```

X <- cbind(1, x)
y <- 0.5 * x + (1.2 + 0.35 * x) * stats::rnorm(length(x))
q_true <- 0.5 * x + (1.2 + 0.35 * x) * stats::qnorm(0.25)

fit_ldvb <- exalStaticLDVB(
  y = y, X = X, p0 = 0.25,
  max_iter = 60, tol = 1e-3,
  verbose = FALSE
)
fit_mcmc <- exalStaticMCMC(
  y = y, X = X, p0 = 0.25,
  n.burn = 60, n.mcmc = 60,
  verbose = FALSE
)
out <- exalStaticDiagnostics(fit_ldvb, fit_mcmc, ref = q_true)
out
plot(out)
plot(out, type = "coefficients")

```

exalStaticLDVB

Static exAL Regression - LDVB Approximation

Description

The function applies a mean-field variational approximation to static Extended Asymmetric Laplace (exAL) regression. Closed-form block updates are combined with a Laplace-Delta approximation for the joint (σ, γ) block, yielding the package's static LDVB routine.

Usage

```

exalStaticLDVB(
  y,
  X,
  p0,
  max_iter = 1000,
  tol = 1e-04,
  b0 = NULL,
  V0 = NULL,
  beta_prior = c("ridge", "rhs", "rhs_ns"),
  beta_prior_controls = NULL,
  a_sigma = 1,
  b_sigma = 1,
  gamma_bounds = c(L.fn(p0), U.fn(p0)),
  log_prior_gamma = NULL,
  init = NULL,
  dqlm.ind = FALSE,
  al.ind = NULL,

```

```

n.samp = 200,
n_samp_xi = 200,
ld_controls = NULL,
vb_control = NULL,
verbose = TRUE
)

```

Arguments

y	Numeric vector (length n).
X	Numeric matrix (n x p).
p0	Target quantile in (0,1).
max_iter	Integer; maximum LDVB iterations (default 1000).
tol	Numeric; convergence tolerance based on relative ELBO changes (default 1e-4).
b0, V0	Prior mean and covariance for $\beta \sim \mathcal{N}(b_0, V_0)$.
beta_prior	Coefficient prior type: "ridge" (default), "rhs" (regularized horseshoe), or "rhs_ns" (Nishimura-Suchard regularized horseshoe with a closed-form inverse-gamma hierarchy for static inference).
beta_prior_controls	Optional list of prior-specific controls. For RHS-family priors (that is, when beta_prior is "rhs" or "rhs_ns"), supported keys include: tau0, nu, s or s2, shrink_intercept, intercept_prec, n_inner, eta_bounds, freeze_tau_iters, freeze_tau_warmup_iters, update_every, update_every_warmup, update_every_warmup_iters, force_tau_after_warmup, collapse_tau_ratio_tol, collapse_beta_max_abs_tol, collapse_invV_med_tol, collapse_beta_l2_tol, collapse_small_beta_frac_tol, small_beta_abs_tol, warn_on_collapse, var_floor, h_curv, verbose, init_lambda, init_log_lambda, init_tau, init_log_tau, init_c2, and init_log_c2. For beta_prior = "rhs_ns", optional slab controls a_zeta, b_zeta, and zeta2_fixed are also supported. In this mode, the local-global-slab block is represented by $(\lambda_j^2, \nu_j, \tau^2, \xi, \zeta^2)$, with closed-form inverse-gamma updates in VB and MCMC. When beta_prior is "rhs" or "rhs_ns", b0 and V0 are retained only for backward-compatible ridge behavior and are ignored for the shrunk coefficients. If both init_log_tau and init_tau are omitted (or NULL), the RHS global scale initializes at tau = 1 (init_log_tau = 0) instead of tau0. By default (shrink_intercept = FALSE), the intercept is excluded from horseshoe shrinkage and uses intercept_prec.
a_sigma, b_sigma	Prior for $\sigma \sim IG(a_\sigma, b_\sigma)$ with density $p(\sigma) \propto \sigma^{-(a_\sigma+1)} e^{-b_\sigma/\sigma}$.
gamma_bounds	Two-vector (L, U) support for gamma. Defaults to c(L.fn(p0), U.fn(p0)).
log_prior_gamma	Function g -> log pi(gamma=g). Default is a truncated Student-t prior centered at 0 on the admissible gamma support.
init	Optional list with starting values: beta, sigma, gamma; if missing, reasonable defaults are used.
dqlm.ind	Logical; if TRUE, fit the reduced AL model (gamma = 0). In that special case the nonconjugate block drops out and the remaining variational updates are available in closed form. This argument is retained for consistency with the dynamic

	exDQLM API; in static examples, <code>al.ind = TRUE</code> is the clearer spelling for this AL special case.
<code>al.ind</code>	Optional static-model alias for <code>dqlm.ind</code> . Prefer this argument when requesting the static AL special case. When supplied, this flag maps directly to <code>dqlm.ind</code> . If both are given, they must agree.
<code>n.samp</code>	Number of samples to draw from the approximated posterior distribution after convergence. Default is <code>n.samp = 200</code> .
<code>n_samp_xi</code>	Integer; retained for backward compatibility in the Laplace-Delta block. Under the current delta-only implementation this value is ignored.
<code>ld_controls</code>	Optional list of controls for the exAL scale-skewness block. Supported keys include <code>optimizer_method</code> ("lbfgsb" or "bfgs"), <code>direct_commit</code> , <code>damping</code> , <code>xi_damping</code> , <code>optimizer_maxit</code> , <code>eig_floor</code> , <code>eig_cap</code> , <code>step_cap_eta</code> , <code>step_cap_ell</code> , <code>eta_lo</code> , <code>eta_hi</code> , <code>sigma_bounds</code> , <code>sigma_init_mode</code> , <code>gamma_init_mode</code> , <code>sigma_floor_abs</code> , <code>sigma_min_mult</code> , <code>sigma_max_mult</code> , <code>sigma_bound_ratio_min</code> , <code>gamma_init_pad_frac</code> , <code>logit_eps</code> , <code>init_cov_diag</code> , <code>reuse_seed</code> , <code>mode_grad_tol</code> , <code>mode_min_eig</code> , <code>auto_stabilize</code> , <code>cycle_window</code> , <code>cycle_lag1_max</code> , <code>cycle_lag2_min</code> , <code>cycle_gamma_min_amp</code> , <code>cycle_sigma_min_amp</code> , <code>cycle_s_min_amp</code> , <code>cycle_tau2_min_amp</code> , <code>stabilize_damping</code> , <code>stabilize_xi_damping</code> , <code>stabilize_step_cap_eta</code> , <code>stabilize_step_cap_ell</code> , and <code>store_trace</code> .
<code>vb_control</code>	Optional normalized VB control list, usually from <code>exal_make_vb_control()</code> . When supplied, the core VB arguments and warmup blocks are read from <code>vb_control</code> first and then merged with the explicit function arguments. When omitted, the package applies its conservative default warmup profile for exAL (<code>sigma</code> , <code>gamma</code>) updates while retaining the built-in RHS-family tau warmup defaults.
<code>verbose</code>	Logical; print progress.

Details

Mean-field factorization:

$$q(\beta) \prod_{i=1}^n q(v_i) q(s_i) q(\sigma, \gamma).$$

This factorization induces a blockwise coordinate-ascent variational inference scheme. The (σ, γ) block is the only nonconjugate component. By default, LDVB uses a structured $q(\gamma)q(\sigma | \gamma)$ factor: `gamma` is represented on the bounded-logit scale $\eta = \text{logit}((\gamma - L)/(U - L))$, and `sigma` is summarized through its conditional GIG moments given `gamma`. This weakens the `gamma`-scale dependence while retaining the same variational target used by the other block updates. The previous two-dimensional Laplace-delta factor on (η, ℓ) with $\ell = \log \sigma$ remains available through `exal_make_vb_sigmagam_control(factorization = "laplace_delta")`. For RHS-family priors, the prior block uses tau warmup/freeze scheduling to avoid the early-collapse regime where global shrinkage drives all slope coefficients toward zero before the likelihood-side variational factors stabilize.

Value

An object with classes "exalStaticLDVB" and "exalStaticFit" containing:

- `qbeta`: list with `m`, `V`.

- `samp.beta`: posterior sample from $q(\beta)$ with `n.samp` rows.
- `qv`: list with `chi` (length `n`), `psi` (scalar), `E_v` and `E_inv_v` (moments).
- `qs`: list with `mu` (length `n`), `tau2` (length `n`), `E_s`, `E_s2`.
- `qsiggam`: list with `eta_hat`, `ell_hat`, `Sigma` (2x2 summary covariance), approximate means `gamma_mean`, `sigma_mean`, the `xi` expectations, and the selected scale-skewness factorization. Under the default structured factor, this list also stores the gamma quadrature grid and conditional GIG scale summaries.
- `samp.sigma`, `samp.gamma`: posterior samples from the variational approximation for the scale and skewness parameters. In the AL special case (`dqlm.ind = TRUE`), `samp.gamma` is a vector of zeros.
- `converged`, `iter`, `run.time`, and `misc` (including `p0`, bounds `L,U`, dimensions, and ELBO trace).
- `beta_prior`: prior metadata and, for RHS-family priors, posterior summaries of the shrinkage hyperparameters, including warmup/freeze-aware tau summaries and collapse diagnostics (`collapse_flag`, `tau_near_zero`, `beta_collapse`, and warning when triggered). For "rhs_ns", the state also tracks `lambda2`, `nu`, `tau2`, `xi`, and `zeta2` with the corresponding inverse moments.
- `diagnostics`: ELBO and joint-convergence diagnostics including a standardized VB iteration trace at `diagnostics$vb_trace` (iteration-wise ELBO / sigma / gamma / convergence deltas), `state/sigma/gamma/ELBO` deltas, stopping reason, and scale-skewness block trace diagnostics, including replicated-xi controls, automatic stabilization / cycle-detection fields, and final local-mode quality checks for the legacy Laplace-delta factor. For RHS fits this also includes `diagnostics$rhs` with the resolved preflight configuration and collapse diagnostics.

Examples

```
set.seed(123)
n <- 60
X <- cbind(1, seq(-1, 1, length.out = n))
y <- as.numeric(X %*% c(0.2, -0.1) + rnorm(n, sd = 0.15))
fit <- exalStaticLDVB(y = y, X = X, p0 = 0.5, max_iter = 60, tol = 1e-3, verbose = FALSE)
fit$converged
head(fit$diagnostics$vb_trace)

fit_rhs <- exalStaticLDVB(
  y = y, X = X, p0 = 0.5,
  beta_prior = "rhs",
  beta_prior_controls = list(tau0 = 0.5, nu = 3, s2 = 1, shrink_intercept = FALSE),
  max_iter = 50, tol = 5e-3, verbose = FALSE
)
fit_rhs$beta_prior$type

fit_rhs_ns <- exalStaticLDVB(
  y = y, X = X, p0 = 0.5,
  beta_prior = "rhs_ns",
  beta_prior_controls = list(tau0 = 0.5, a_zeta = 1.5, b_zeta = 1, zeta2_fixed = 1),
  max_iter = 50, tol = 5e-3, verbose = FALSE
)
fit_rhs_ns$beta_prior$type
```

```

fit_al <- exalStaticLDVB(
  y = y, X = X, p0 = 0.5,
  al.ind = TRUE,
  max_iter = 50, tol = 5e-3, verbose = FALSE
)
fit_al$dqlm.ind

```

exalStaticMCMC	<i>exAL (static) - MCMC algorithm</i>
----------------	---------------------------------------

Description

The function applies a Gibbs sampler for static Extended Asymmetric Laplace regression (exAL). We update β, v, s from their full conditionals, then update (σ, γ) either jointly on transformed coordinates $(\ell, \eta) = (\log \sigma, \text{logit}((\gamma - L)/(U - L)))$ (for "rw" and "laplace_rw"), with a scale-collapsed gamma transition (the default), or with legacy univariate gamma kernels ("slice", "slice_eta", "laplace_local"). Optional multi-refresh and global-jump controls are available to improve exAL mixing in hard cases.

Usage

```

exalStaticMCMC(
  y,
  X,
  p0,
  b0 = NULL,
  v0 = NULL,
  beta_prior = c("ridge", "rhs", "rhs_ns"),
  beta_prior_controls = NULL,
  a_sigma = 1,
  b_sigma = 1,
  gamma_bounds = c(L.fn(p0), U.fn(p0)),
  log_prior_gamma = NULL,
  init = NULL,
  dqlm.ind = FALSE,
  al.ind = NULL,
  n.burn = 2000,
  n.mcmc = 1500,
  thin = 1,
  init.from.vb = FALSE,
  vb_init_controls = NULL,
  vb_init_fit = NULL,
  mcmc_control = NULL,
  sigmagam_controls = NULL,
  mh.proposal = c("collapsed_slice", "slice", "laplace_rw", "rw", "slice_eta",
    "laplace_local"),

```

```

mh.adapt = TRUE,
mh.adapt.interval = 50L,
mh.target.accept = c(0.2, 0.45),
mh.scale.bounds = c(0.1, 10),
mh.max_scale.step = 0.35,
mh.min_burn_adapt = 50L,
slice.width = 0.1,
slice.max.steps = Inf,
gamma.substeps = 1L,
p.global.eta.jump = 0,
global.eta.jump.scale = 1,
trace.diagnostics = TRUE,
trace.every = 1L,
verbose = TRUE,
progress_callback = NULL
)

```

Arguments

<code>y</code>	Numeric vector of length n .
<code>X</code>	Numeric matrix $n \times p$ (design).
<code>p0</code>	Quantile level in $(0, 1)$.
<code>b0, V0</code>	Prior mean and covariance for β (Normal). Defaults: $b_0 = \mathbf{0}_p$, $V_0 = 10^6 I_p$.
<code>beta_prior</code>	Coefficient prior type: "ridge" (default), "rhs" (regularized horseshoe), or "rhs_ns" (Nishimura-Suchard regularized horseshoe with a closed-form inverse-gamma hierarchy for static inference).
<code>beta_prior_controls</code>	Optional list of prior-specific controls. For RHS-family priors (that is, when <code>beta_prior</code> is "rhs" or "rhs_ns"), supported keys include: <code>tau0</code> , <code>nu</code> , <code>s</code> or <code>s2</code> , <code>shrink_intercept</code> , <code>intercept_prec</code> , <code>n_inner</code> , <code>eta_bounds</code> , <code>var_floor</code> , <code>h_curv</code> , <code>verbose</code> , <code>init_lambda</code> , <code>init_log_lambda</code> , <code>init_tau</code> , <code>init_log_tau</code> , <code>init_c2</code> , <code>init_log_c2</code> , <code>collapse_tau_ratio_tol</code> , <code>collapse_beta_max_abs_tol</code> , <code>collapse_invV_med_tol</code> , <code>collapse_beta_l2_tol</code> , <code>collapse_small_beta_frac_tol</code> , <code>small_beta_abs_tol</code> , <code>slice_width</code> , and <code>slice_max_steps</code> . For <code>beta_prior = "rhs_ns"</code> , optional slab controls <code>a_zeta</code> , <code>b_zeta</code> , and <code>zeta2_fixed</code> are also supported. In this mode, the local-global-slab block is represented by $(\lambda_j^2, \nu_j, \tau_j^2, \xi, \zeta^2)$ and updated with closed-form Gibbs steps. When <code>beta_prior</code> is "rhs" or "rhs_ns", <code>b0</code> and <code>V0</code> are ignored for the shrunk coefficients and retained only for backward-compatible ridge behavior. If both <code>init_log_tau</code> and <code>init_tau</code> are omitted (or NULL), the RHS global scale initializes at <code>tau = 1</code> (<code>init_log_tau = 0</code>) instead of <code>tau0</code> . By default (<code>shrink_intercept = FALSE</code>), the intercept is excluded from horseshoe shrinkage and uses <code>intercept_prec</code> .
<code>a_sigma, b_sigma</code>	Hyperparameters for an inverse-gamma prior on <code>sigma</code> , with density proportional to $\sigma^{-(a_sigma+1)} \exp(-b_sigma/\sigma)$.
<code>gamma_bounds</code>	Numeric length-2 vector (L, U) for <code>gamma</code> . Defaults to <code>c(L.fn(p0), U.fn(p0))</code> .

log_prior_gamma	Function <code>function(g) log pi(g)</code> for gamma on (L, U). Default is a truncated Student-t prior centered at 0 on the admissible support.
init	Optional list with starting values: beta, sigma, gamma, v (length n), s (length n), and for RHS-family priors optionally lambda, tau, and c2. For <code>beta_prior = "rhs_ns"</code> , the squared-scale parameterization lambda2, tau2, zeta2, and optional auxiliaries nu, xi are also accepted. Missing pieces are filled sensibly.
dqlm.ind	Logical; if TRUE, fit the reduced AL model (<code>gamma = 0</code>), corresponding to Bayesian linear quantile regression under the AL working likelihood. This removes the gamma- and s-blocks and leaves conjugate Gibbs updates for beta, sigma, and v. This argument is retained for consistency with the dynamic exDQLM API; in static examples, <code>al.ind = TRUE</code> is the clearer spelling for this AL special case.
al.ind	Optional static-model alias for <code>dqlm.ind</code> . Prefer this argument when requesting the static AL special case. When supplied, this flag maps directly to <code>dqlm.ind</code> . If both are given, they must agree.
n.burn	Number of burn-in iterations. Default 2000.
n.mcmc	Number of kept MCMC iterations (after burn). Default 1500.
thin	Integer; save every thin-th iteration after burn. We internally run <code>n.burn + n.mcmc * thin</code> iterations to return exactly <code>n.mcmc</code> saved draws.
init.from.vb	Logical; if TRUE, run static VB first and use its posterior moments as MCMC initialization.
vb_init_controls	Optional list controlling VB warm start. Supported keys: <code>max_iter</code> , <code>tol</code> , <code>n_samp_xi</code> , <code>verbose</code> , and <code>ld_controls</code> (passed through to <code>exalStaticLDVB()</code>).
vb_init_fit	Optional precomputed static VB fit object used as the warm-start reference when <code>init.from.vb = TRUE</code> .
mcmc_control	Optional normalized MCMC control list, usually from <code>exal_make_mcmc_control()</code> . When supplied, the core MCMC arguments and warmup blocks are read from <code>mcmc_control</code> first and then merged with the explicit function arguments. When omitted, the package applies its conservative default exAL (sigma, gamma) warmup profile and keeps the RHS-family tau warmup defaults active through the shared prior layer.
sigmagam_controls	Optional list controlling warmup/freeze behavior for the nonconjugate (sigma, gamma) block. Prefer <code>exal_make_mcmc_sigmagam_control()</code> or the sigmagam block of <code>exal_make_mcmc_control()</code> for new code; this argument remains available as a direct advanced override.
mh.proposal	Character string controlling the exAL nonconjugate update kernel. "collapsed_slice" (default) integrates out sigma for the bounded gamma slice step on transformed eta and then redraws sigma from its exact GIG conditional. "slice" uses the previous exact conditional sigma draw followed by bounded slice sampling on gamma, and "slice_eta" does the same on transformed eta. "laplace_rw" uses a Laplace-informed adaptive random-walk MH update on the transformed joint block $(\eta, \ell) = (\text{logit}((\gamma - L)/(U - L)), \log \sigma)$. "rw" uses the same exact joint update with identity base covariance. "laplace_local" reproduces the prior approximate local-Gaussian gamma draw retained for compatibility and not recommended for routine use. Only "laplace_local" is approximate.

<code>mh.adapt</code>	Logical; adapt the random-walk proposal scale during burn-in for "rw" and "laplace_rw". Ignored for "collapsed_slice", "laplace_local", "slice", and "slice_eta".
<code>mh.adapt.interval</code>	Integer adaptation window for RW-based kernels.
<code>mh.target.accept</code>	Numeric length-2 target acceptance band.
<code>mh.scale.bounds</code>	Numeric length-2 lower/upper bounds for RW proposal scale multiplier.
<code>mh.max_scale.step</code>	Numeric multiplicative adaptation cap in $(0, 1)$.
<code>mh.min_burn_adapt</code>	Integer minimum burn-in before adaptation starts.
<code>slice.width</code>	Positive numeric width for bounded slice updates when <code>mh.proposal</code> is "collapsed_slice", "slice", or "slice_eta".
<code>slice.max.steps</code>	Positive integer or Inf; maximum stepping-out expansions for the slice sampler.
<code>gamma.substeps</code>	Positive integer; number of consecutive gamma-kernel refreshes per outer MCMC iteration. Default 1.
<code>p.global.eta.jump</code>	Numeric in $[0, 1]$; per-substep probability of proposing a global independence-MH move on eta (the logit transform of gamma) using a Laplace proposal with MH correction. Default 0.
<code>global.eta.jump.scale</code>	Positive numeric scale multiplier applied to the Laplace proposal SD used in global eta jumps.
<code>trace.diagnostics</code>	Logical; if TRUE, retain per-iteration gamma/s diagnostics under <code>mh.diagnostics\$trace</code> . Set FALSE for lighter-weight runs.
<code>trace.every</code>	Positive integer; when <code>trace.diagnostics=TRUE</code> , record one diagnostics row every <code>trace.every</code> iterations.
<code>verbose</code>	Print progress every <code>progress_every</code> iterations.
<code>progress_callback</code>	Optional callback invoked with a named list at MCMC start, at each progress checkpoint, and on completion. Intended for workflow-level per-case progress logging.

Value

An object with classes "exalStaticMCMC" and "exalStaticFit" containing:

- `run.time` - total wall time in seconds.
- `X, p0, bounds` - design, quantile, and (L, U) .
- `samp.beta` - posterior sample of beta as `coda: :mcmc (n.mcmc x p)`.
- `samp.sigma` - posterior sample of sigma as `coda: :mcmc`.

- `samp.gamma` - posterior sample of gamma as `coda::mcmc`.
- `samp.v` - latent `v` draws as `coda::mcmc (n.mcmc x n)`.
- `samp.s` - latent `s` draws as `coda::mcmc (n.mcmc x n)`.
- `samp.lambda`, `samp.tau`, `samp.c2` - RHS latent draws when an RHS-family prior is used; otherwise NULL.
- `beta_prior` - prior metadata and, for RHS-family priors, posterior summaries of the shrinkage block. For "rhs_ns", the state tracks `lambda2`, `nu`, `tau2`, `xi`, and `zeta2`.
- `mh.diagnostics` - proposal kernel diagnostics for the exAL gamma update, including whether the saved kernel is exact/signoff-ready.
- `rhs.diagnostics` - RHS latent summaries and optional trace metadata when an RHS-family prior is used, including the resolved preflight configuration used at fit start.
- `last` - last state of the chain (useful for restarts).

Examples

```
set.seed(123)
n <- 60; p <- 3
X <- cbind(1, rnorm(n), rnorm(n))
beta0 <- c(0.5, -1, 0.8); sigma0 <- 1.2
y <- as.numeric(X %*% beta0 + rnorm(n, 0, sigma0))
fit <- exalStaticMCMC(
  y, X, p0 = 0.5, n.burn = 60, n.mcmc = 60, thin = 1, verbose = FALSE
)
summary(fit$samp.beta)

fit_rhs <- exalStaticMCMC(
  y, X, p0 = 0.5,
  beta_prior = "rhs",
  beta_prior_controls = list(tau0 = 0.5, nu = 3, s2 = 1, shrink_intercept = FALSE),
  n.burn = 50, n.mcmc = 50, thin = 1, verbose = FALSE
)
fit_rhs$beta_prior$type

fit_rhs_ns <- exalStaticMCMC(
  y, X, p0 = 0.5,
  beta_prior = "rhs_ns",
  beta_prior_controls = list(tau0 = 0.5, a_zeta = 1.5, b_zeta = 1, zeta2_fixed = 1),
  n.burn = 40, n.mcmc = 40, thin = 1, verbose = FALSE
)
fit_rhs_ns$beta_prior$type

fit_al <- exalStaticMCMC(
  y, X, p0 = 0.5,
  al.ind = TRUE,
  n.burn = 50, n.mcmc = 50, thin = 1, verbose = FALSE
)
fit_al$ddqlm.ind
```

exal_make_mcmc_control

Build advanced MCMC control

Description

Returns a readable mcmc_control list for [exalStaticMCMC\(\)](#) and [exdqlmMCMC\(\)](#). This keeps the warmup surface explicit instead of relying on ad hoc nested lists.

Usage

```
exal_make_mcmc_control(
  n_burn = 2000L,
  n_mcmc = 1500L,
  thin = 1L,
  verbose = FALSE,
  progress_every = NULL,
  init_from_vb = TRUE,
  vb_warm_start_control = NULL,
  sigmagam = NULL,
  theta = NULL,
  latent_state = NULL,
  dqlm_sigma = NULL,
  control = NULL
)
```

Arguments

n_burn, n_mcmc, thin, verbose	Core MCMC controls.
progress_every	Optional progress cadence for callers that support it.
init_from_vb	Logical; initialize from a VB warm start.
vb_warm_start_control	Optional VB warm-start control list, often from exal_make_vb_control() .
sigmagam	Optional list, usually from exal_make_mcmc_sigmagam_control() .
theta	Optional list, usually from exal_make_mcmc_theta_control() .
latent_state	Optional list, usually from exal_make_mcmc_latent_state_control() .
dqlm_sigma	Optional list, usually from exal_make_mcmc_dqlm_sigma_control() .
control	Optional existing control list to update.

Value

A normalized list suitable for mcmc_control.

exal_make_mcmc_dqlm_sigma_control

Build DQLM sigma-only MCMC warmup control

Description

Returns a normalized mcmc_control\$dqlm_sigma block for `exdqlmMCMC()` in the reduced AL / DQLM branch.

Usage

```
exal_make_mcmc_dqlm_sigma_control(
  freeze_burnin_iters = 0L,
  freeze_only_during_burn = TRUE,
  force_after_warmup = TRUE,
  trace = TRUE
)
```

Arguments

freeze_burnin_iters	Non-negative integer; number of burn-in iterations to hold the sigma-only block fixed.
freeze_only_during_burn	Logical; if TRUE, hard freeze only applies during burn-in.
force_after_warmup	Logical; force one immediate post-warmup update.
trace	Logical; record diagnostics traces.

Value

A normalized list suitable for mcmc_control\$dqlm_sigma.

exal_make_mcmc_latent_state_control

Build dynamic MCMC latent-state warmup control

Description

Returns a normalized mcmc_control\$latent_state block for `exdqlmMCMC()`.

Usage

```
exal_make_mcmc_latent_state_control(
  mode = c("u_only", "u_st_pair"),
  freeze_burnin_iters = 0L,
  freeze_only_during_burn = TRUE,
  force_after_warmup = TRUE,
  min_postwarmup_updates = 0L,
  trace = TRUE
)
```

Arguments

mode	One of "u_only" or "u_st_pair".
freeze_burnin_iters	Non-negative integer; number of burn-in iterations to hold the latent-state block fixed.
freeze_only_during_burn	Logical; if TRUE, hard freeze only applies during burn-in.
force_after_warmup	Logical; force one immediate post-warmup update.
min_postwarmup_updates	Non-negative integer; minimum number of post-warmup updates required before chain-health style gates can fire.
trace	Logical; record diagnostics traces.

Value

A normalized list suitable for `mcmc_control$latent_state`.

```
exal_make_mcmc_sigmagam_control
```

Build MCMC sigmagam warmup control

Description

Returns a normalized `mcmc_control$sigmagam` block for `exalStaticMCMC()` and `exdqImMCMC()`.

Usage

```
exal_make_mcmc_sigmagam_control(
  freeze_burnin_iters = NULL,
  freeze_only_during_burn = NULL,
  force_after_warmup = NULL,
  delay_adapt_until_after_warmup = NULL,
  delay_laplace_refresh_until_after_warmup = NULL
)
```

Arguments

freeze_burnin_iters
Non-negative integer; number of burn-in iterations to hold the (sigma, gamma) block fixed.

freeze_only_during_burn
Logical; if TRUE, hard freeze only applies during burn-in.

force_after_warmup
Logical; force one post-warmup update.

delay_adapt_until_after_warmup
Logical; keep proposal adaptation off until warmup ends.

delay_laplace_refresh_until_after_warmup
Logical; keep Laplace refresh off until warmup ends.

Value

A normalized list suitable for mcmc_control\$sigmagam.

When called with no arguments, this returns the package's conservative default exAL (sigma, gamma) MCMC warmup profile.

exal_make_mcmc_theta_control

Build MCMC theta warmup control

Description

Returns a normalized mcmc_control\$theta block for `exdq1mMCMC()`.

Usage

```
exal_make_mcmc_theta_control(
  enabled = FALSE,
  freeze_burnin_iters = 0L,
  freeze_only_during_burn = TRUE,
  sparse_update_every = 1L,
  sparse_update_until_iter = 0L,
  force_first_postwarmup_update = TRUE,
  trace = TRUE
)
```

Arguments

enabled
Logical; explicit on/off switch.

freeze_burnin_iters
Non-negative integer; number of burn-in iterations to hold the theta block fixed.

freeze_only_during_burn
Logical; if TRUE, hard freeze only applies during burn-in.

sparse_update_every	Positive integer; sparse-update period during the warmup window.
sparse_update_until_iter	Non-negative integer; last iteration where the sparse schedule is active.
force_first_postwarmup_update	Logical; force one update immediately after the hard freeze / sparse schedule ends.
trace	Logical; record diagnostics traces.

Value

A normalized list suitable for `mcmc_control$theta`.

`exal_make_vb_control` *Build advanced VB control*

Description

Returns a readable `vb_control` list for `exalStaticLDVB()` and `exdqlmLDVB()`. This keeps the warmup surface explicit instead of relying on ad hoc nested lists.

Usage

```
exal_make_vb_control(
  max_iter = 150L,
  tol = 1e-04,
  n_samp_xi = 200L,
  verbose = FALSE,
  sigmagam = NULL,
  sts = NULL,
  control = NULL
)
```

Arguments

<code>max_iter</code> , <code>tol</code> , <code>n_samp_xi</code> , <code>verbose</code>	Core VB controls.
<code>sigmagam</code>	Optional list, usually from <code>exal_make_vb_sigmagam_control()</code> .
<code>sts</code>	Optional list, usually from <code>exal_make_vb_sts_control()</code> , for the dynamic latent <code>s_t</code> block in <code>exdqlmLDVB()</code> .
<code>control</code>	Optional existing control list to update.

Value

A normalized list suitable for `vb_control`.

exal_make_vb_sigmagam_control

Build VB sigmagam warmup control

Description

Returns a normalized sigmagam block for vb_control lists used by [exalStaticLDVB\(\)](#), [exdqlmLDVB\(\)](#), and VB warm-start paths in [exalStaticMCMC\(\)](#) and [exdqlmMCMC\(\)](#).

Usage

```
exal_make_vb_sigmagam_control(
    factorization = NULL,
    structured_grid_size = NULL,
    structured_span_sd = NULL,
    freeze_warmup_iters = NULL,
    force_after_warmup = NULL,
    postwarmup_damping = NULL,
    postwarmup_damping_iters = NULL,
    min_postwarmup_updates = NULL
)
```

Arguments

factorization	Character; "structured" uses the $q(\gamma) q(\sigma \gamma)$ scale-skewness factorization. The legacy two-dimensional Laplace-delta factor can be requested with "laplace_delta".
structured_grid_size	Odd integer; number of quadrature nodes for the structured gamma factor. The package default is 151.
structured_span_sd	Numeric; local quadrature half-width in curvature standard deviations for the structured gamma factor.
freeze_warmup_iters	Non-negative integer; number of early VB iterations during which the (σ, γ) block is held fixed.
force_after_warmup	Logical; force one immediate post-warmup update.
postwarmup_damping	Numeric in $(0, 1]$; damping applied after warmup.
postwarmup_damping_iters	Non-negative integer; number of damped post-warmup iterations.
min_postwarmup_updates	Non-negative integer; minimum number of post-warmup updates required before convergence-style gates can fire.

Value

A normalized list suitable for vb_control\$sigmagam.

When called with no arguments, this returns the package's conservative default exAL (sigma, gamma) warmup profile.

exal_make_vb_sts_control

Build dynamic VB latent-state warmup control

Description

Returns a normalized sts block for vb_control lists used by `exdq1mLDVB()`.

Usage

```
exal_make_vb_sts_control(
  freeze_warmup_iters = 0L,
  force_after_warmup = TRUE,
  min_postwarmup_updates = 0L
)
```

Arguments

freeze_warmup_iters

Non-negative integer; number of early VB iterations during which the latent s_t block is held fixed.

force_after_warmup

Logical; force one immediate post-warmup update.

min_postwarmup_updates

Non-negative integer; minimum number of post-warmup updates required before convergence-style gates can fire.

Value

A normalized list suitable for vb_control\$sts.

exdqlmDiagnostics	<i>exDQLM Diagnostics</i>
-------------------	---------------------------

Description

The function computes the following for the model(s) provided: the posterior predictive loss criterion based off the check loss, the CRPS approximated as a finite integrated quantile score over posterior predictive empirical quantiles, the one-step-ahead distribution sequence, and deterministic semiclosed KL normality diagnostics for the MAP standardized forecast errors. The returned diagnostic object can be printed, summarized, or plotted with standard methods. Calling `plot()` on the object produces the QQ plot and ACF plot corresponding to the one-step-ahead distribution sequence, together with a time series plot of the MAP standard forecast errors.

Usage

```
exdqlmDiagnostics(
  m1,
  m2 = NULL,
  plot = FALSE,
  cols = c("red", "blue"),
  ref = NULL,
  crps_probs = seq(0.01, 0.99, by = 0.01),
  crps_weights = NULL,
  kl_k = NULL
)
```

Arguments

<code>m1</code>	A fitted dynamic <code>exdqlmFit</code> object, such as an object returned by exdqlmLTVB , exdqlmMCMC , or legacy exdqlmISVB .
<code>m2</code>	An optional second fitted dynamic <code>exdqlmFit</code> object to compare with <code>m1</code> .
<code>plot</code>	Logical value indicating whether to immediately plot the returned diagnostic object as a convenience shortcut. Default is <code>FALSE</code> ; the preferred workflow is to save the object and then call <code>plot()</code> on it.
<code>cols</code>	Character vector of length 1 or 2 giving color(s) used to plot diagnostics. Default <code>c("red", "blue")</code> .
<code>ref</code>	Optional finite reference sample of size <code>length(m1\$y)</code> from a standard normal distribution. Used for the reversed KL diagnostic. When <code>NULL</code> , a deterministic standard-normal quantile grid is used.
<code>crps_probs</code>	Numeric vector of quantile levels used to approximate CRPS through the integrated quantile-score identity. Values must be strictly between 0 and 1. Default is <code>seq(0.01, 0.99, by = 0.01)</code> .
<code>crps_weights</code>	Optional non-negative numeric weights for <code>crps_probs</code> . When <code>NULL</code> , equal weights are used. When provided, weights are normalized to sum to 1.

`kl_k` Optional positive integer vector of nearest-neighbor values used for the KL entropy and cross-entropy estimates. When NULL, the default grid `c(3, 5, 10, 20, 30)` is filtered to values supported by the finite standardized-error sample size, falling back to 1 for very small samples.

Details

The primary KL summary is computed from the MAP standardized one-step-ahead forecast errors `map.standard.forecast.errors`. The reported KL value is the user-facing calibration diagnostic and estimates $KL(P_e || N(0, 1))$, where P_e is the continuous diagnostic-error law represented by the standardized errors. It uses the semiclosed identity $KL(P_e || N(0, 1)) = CE(P_e, N(0, 1)) - H(P_e)$, with the normal cross-entropy term evaluated analytically and the entropy estimated by a one-dimensional k-nearest-neighbor estimator. The reported `KL.flip` estimates the reversed diagnostic $KL(N(0, 1) || P_e)$ using kNN cross-entropy. The reversed direction is more sensitive and should be read as a secondary sensitivity diagnostic, not as a replacement for KL. Advanced by-k sensitivity tables and Gaussian plug-in checks are stored under `kl.details` so the top-level diagnostic object exposes a single primary KL value. Negative finite-sample estimates are not clamped; they indicate estimator bias or instability for the current sample.

Value

An object of class "exdqlmDiagnostic" containing the following:

- `m1.uts` - The one-step-ahead distribution sequence of `m1`.
- `m1.KL` - The forward KL normality diagnostic $KL(P_{\text{error}} || N(0, 1))$ for the MAP standardized forecast errors.
- `m1.KL.flip` - The reversed ("flipped") KL diagnostic $KL(N(0, 1) || P_{\text{error}})$ for the MAP standardized forecast errors; this is a secondary sensitivity diagnostic.
- `m1.CRPS` - The mean CRPS approximated by a finite integrated quantile score over posterior predictive empirical quantiles.
- `m1.pplc` - The posterior predictive loss criterion of `m1` based off the check loss function.
- `m1.qq` - The ordered pairs of the qq-plot comparing `m1.uts` with a standard normal distribution.
- `m1.acf` - The autocorrelations of `m1.uts` by lag.
- `m1.rt` - Run-time of the original model `m1` in seconds.
- `m1.msfe` - MAP standardized one-step-ahead forecast errors from the original model `m1`.
- `y` - The original time-series used to fit `m1`.
- `crps.method` - The CRPS approximation method.
- `crps.probs` - The quantile levels used for the CRPS approximation.
- `crps.weights` - The normalized weights used for the CRPS approximation.
- `kl.method`, `kl.k`, `kl.aggregate`, and `kl.reference` - KL estimator metadata.
- `kl.n_finite`, `kl.n_ref`, and `kl.zero_distance_count` - KL diagnostic sample-size and distance-floor metadata.
- `kl.details` - Advanced KL estimator details by model. For each model this includes primary/flipped definitions, by-k sensitivity tables, a Gaussian plug-in check, and estimator metadata.

If `m2` is provided, analogous results for `m2` are also included in the list.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.95), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
M0.diags = exdqlmDiagnostics(M0)
M0.diags
plot(M0.diags)
options(old)
```

exdqlmForecast	<i>k-step-ahead quantile forecasts</i>
----------------	--

Description

Computes filtered and k -step-ahead forecast quantiles from a fitted dynamic quantile model. The returned `exdqlmForecast` object can be printed, summarized, plotted with `plot()`, or passed to [diagnostics](#) with held-out observations.

Usage

```
exdqlmForecast(
  start.t,
  k,
  m1,
  fFF = NULL,
  fGG = NULL,
  plot = FALSE,
  add = FALSE,
  cols = c("purple", "magenta"),
  cr.percent = 0.95,
  return.draws = FALSE,
  n.samp = NULL,
  seed = NULL
)
```

Arguments

<code>start.t</code>	Integer index at which forecasts start (must be within the span of the fitted model in <code>m1</code>).
----------------------	---

<code>k</code>	Integer number of steps ahead to forecast.
<code>m1</code>	A fitted dynamic <code>exdqImFit</code> object, such as an object returned by <code>exdqImLDVB()</code> , <code>exdqImMCMC()</code> , or legacy <code>exdqImISVB()</code> .
<code>fff</code>	Optional state vector(s) for the forecast steps. A numeric matrix with q rows and either 1 column (non–time-varying) or k columns (time-varying). Its dimension must match the fitted model in <code>m1</code> .
<code>fgg</code>	Optional evolution matrix/matrices for the forecast steps. Either a numeric $q \times q$ matrix (non–time-varying) or a $q \times q \times k$ array (time-varying). Its dimensions must match the fitted model in <code>m1</code> .
<code>plot</code>	Logical value indicating whether to immediately plot filtered and forecast quantiles with equal–tailed credible intervals. Default is <code>FALSE</code> ; the preferred workflow is to save the returned object and call <code>plot()</code> on it.
<code>add</code>	Logical value indicating whether to add the forecasted quantiles to the current plot. Default is <code>FALSE</code> .
<code>cols</code>	Character vector of length 2 giving the colors for filtered and forecasted quantiles respectively. Default <code>c("purple", "magenta")</code> .
<code>cr.percent</code>	Numeric in $(0, 1)$ indicating the probability mass for the credible intervals (e.g., <code>0.95</code>). Default <code>0.95</code> .
<code>return.draws</code>	Logical; if <code>TRUE</code> , the function also returns a matrix of posterior predictive forecast draws in <code>samp.fore</code> . Default is <code>FALSE</code> .
<code>n.samp</code>	Optional positive integer specifying how many forecast draws to return when <code>return.draws = TRUE</code> . If omitted, all available posterior (σ, γ) draws from <code>m1</code> are used.
<code>seed</code>	Optional integer random seed used only for forecast-draw generation when <code>return.draws = TRUE</code> . If provided, the previous <code>R</code> RNG state is restored on exit.

Value

An object of class "exdqImForecast" containing the following:

- `start.t` Integer index at which forecasts start (within the span of the fitted model in `m1`).
- `k` Integer number of steps ahead forecasted.
- `m1` The fitted exDQLM model object used to initialize the forecast.
- `cr.percent` The probability mass for the credible intervals (e.g., `0.95`).
- `fa` Forecast state mean vectors ($q \times k$ matrix).
- `fR` Forecast state covariance matrices ($q \times q \times k$ array).
- `ff` Forecast quantile means (length- k numeric).
- `fQ` Forecast quantile variances (length- k numeric).
- `samp.fore` Optional posterior predictive forecast draws ($k \times n.samp$) returned when `return.draws = TRUE`.

Examples

```
# Toy example
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 20L)
y = scIVTmag[1:100]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
                dqlm.ind = TRUE, sig.init = 15, n.samp = 30,
                verbose = FALSE)
M0.forecast = predict(M0, start.t = 90, k = 10,
                     return.draws = TRUE, n.samp = 50, seed = 123)

M0.forecast
plot(M0.forecast)
dim(M0.forecast$samp.fore)
options(old)
```

exdqlmForecastDiagnostics

Held-out forecast diagnostics for exDQLM forecasts

Description

Computes held-out forecast scores from one or two `exdqlmForecast` objects returned by `exdqlmForecast()`. Unlike `exdqlmDiagnostics()`, which summarizes fitted one-step-ahead forecast errors and their KL normality diagnostics, this function evaluates posterior predictive forecast draws against observations reserved outside the fitted sample.

Usage

```
exdqlmForecastDiagnostics(
  m1,
  m2 = NULL,
  y,
  p0 = NULL,
  crps_probs = seq(0.01, 0.99, by = 0.01),
  crps_weights = NULL
)
```

Arguments

- | | |
|-----------------|--|
| <code>m1</code> | An object of class "exdqlmForecast", returned by <code>exdqlmForecast()</code> with <code>return.draws = TRUE</code> . |
| <code>m2</code> | An optional second object of class "exdqlmForecast" to compare with <code>m1</code> . |
| <code>y</code> | Numeric vector or time series of held-out observations. Its length must equal the forecast horizon. |

<code>p0</code>	Optional quantile level used for the check-loss calculation. When NULL, the value is taken from <code>m1\$m1\$p0</code> . If <code>m2</code> is supplied, its fitted quantile level must agree with the resolved value.
<code>crps_probs</code>	Numeric vector of quantile levels used to approximate CRPS through the integrated quantile-score identity. Values must be strictly between 0 and 1. Default is <code>seq(0.01, 0.99, by = 0.01)</code> .
<code>crps_weights</code>	Optional non-negative numeric weights for <code>crps_probs</code> . When NULL, equal weights are used. When provided, weights are normalized to sum to 1.

Details

The check loss is computed at the target quantile level `p0` using the forecast quantile means `ff` stored in each forecast object. CRPS is computed from `samp.fore` using the same finite integrated quantile-score approximation used by `exdqlmDiagnostics()`. This function does not compute KL diagnostics because KL in `exdqlm` is defined for fitted one-step-ahead MAP standardized forecast errors, not for arbitrary held-out forecast draws.

Value

An object of class "exdqlmForecastDiagnostic" containing:

- `y` - Held-out observations used for scoring.
- `p0` - Quantile level used for check loss.
- `horizon` - Forecast horizon.
- `m1.check_loss` - Mean target-quantile check loss for `m1`.
- `m1.CRPS` - Mean CRPS approximation for `m1`.
- `m1.pointwise` - Pointwise held-out scores for `m1`.
- `crps.method`, `crps.probs`, and `crps.weights` - CRPS approximation metadata.

If `m2` is supplied, analogous `m2.*` fields are included.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:65]
y_train = y[1:60]
y_holdout = y[61:65]
model = polytrendMod(1, stats::quantile(y_train, 0.85), 10)
M0 = exdqlmLDVB(y_train, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
  dqlm.ind = TRUE, sig.init = 15,
  n.samp = 20, tol = 0.2, verbose = FALSE)
fFF = model$FF[, 1, drop = FALSE]
fGG = model$GG
M0.forecast = exdqlmForecast(start.t = 60, k = 5, m1 = M0,
  fFF = fFF, fGG = fGG,
  return.draws = TRUE, n.samp = 20, seed = 123,
  plot = FALSE)
score <- exdqlmForecastDiagnostics(M0.forecast, y = y_holdout)
```

```
score
options(old)
```

exdqlmISVB

exDQLM - legacy ISVB algorithm

Description

The function applies an Importance Sampling Variational Bayes (ISVB) algorithm to estimate the posterior of an exDQLM. This legacy VB engine is retained for backward compatibility and historical comparisons; for standard exDQLM VB fits, [exdqlmLDVB\(\)](#) is the main default technique.

Usage

```
exdqlmISVB(
  y,
  p0,
  model,
  df,
  dim.df,
  fix.gamma = FALSE,
  gam.init = NA,
  fix.sigma = FALSE,
  sig.init = NA,
  dqlm.ind = FALSE,
  exps0,
  tol = 0.1,
  n.IS = 500,
  n.samp = 200,
  PriorSigma = NULL,
  PriorGamma = NULL,
  verbose = TRUE,
  debug_shapes = FALSE,
  debug_every = 5
)
```

Arguments

<code>y</code>	A univariate time-series.
<code>p0</code>	The quantile of interest, a value between 0 and 1.
<code>model</code>	List of the state-space model including GG, FF, prior parameters <code>m0</code> and <code>C0</code> .
<code>df</code>	Discount factors for each block.
<code>dim.df</code>	Dimension of each block of discount factors.
<code>fix.gamma</code>	Logical value indicating whether to fix gamma at <code>gam.init</code> . Default is FALSE.

<code>gam.init</code>	Initial value for gamma (skewness parameter), or value at which gamma will be fixed if <code>fix.gamma=TRUE</code> .
<code>fix.sigma</code>	Logical value indicating whether to fix sigma at <code>sig.init</code> . Default is <code>FALSE</code> .
<code>sig.init</code>	Initial value for sigma (scale parameter), or value at which sigma will be fixed if <code>fix.sigma=TRUE</code> .
<code>dqlm.ind</code>	Logical value indicating whether to fix gamma at 0, reducing the exDQLM to the special case of the DQLM. Default is <code>FALSE</code> .
<code>exps0</code>	Initial value for dynamic quantile. If <code>exps0</code> is not specified, it is set to the DLM estimate of the p_0 quantile.
<code>tol</code>	Tolerance for convergence of dynamic quantile estimates. Default is <code>tol=0.1</code> .
<code>n.IS</code>	Number of particles for the importance sampling of joint variational distribution of sigma and gamma. Default is <code>n.IS=500</code> .
<code>n.samp</code>	Number of samples to draw from the approximated posterior distribution. Default is <code>n.samp=200</code> .
<code>PriorSigma</code>	List of parameters for inverse gamma prior on sigma; shape <code>a_sig</code> and scale <code>b_sig</code> . Default is an inverse gamma with mean 1 (or <code>sig.init</code> if provided) and variance 10.
<code>PriorGamma</code>	List of parameters for truncated student-t prior on gamma; center <code>m_gam</code> , scale <code>s_gam</code> and degrees of freedom <code>df_gam</code> . Default is a standard student-t with 1 degree of freedom, truncated to the support of gamma.
<code>verbose</code>	Logical value indicating whether progress should be displayed.
<code>debug_shapes</code>	Logical; if <code>TRUE</code> , print KF input/output shapes every <code>debug_every</code> iterations.
<code>debug_every</code>	Integer; frequency (in iterations) for shape prints when <code>debug_shapes=TRUE</code> .

Details

Advanced options (set via `options()`):

- `exdqlm.use_cpp_kf`: use the C++ Kalman filter bridge (default `TRUE`).
- `exdqlm.compute_elbo`: compute ELBO every iteration (default `TRUE`).
- `exdqlm.tol_elbo`: ELBO convergence tolerance (default `1e-6`).
- `exdqlm.tol_sigma`: sigma-delta convergence tolerance (default: `tol`).
- `exdqlm.tol_gamma`: gamma-delta convergence tolerance (default: `tol`).
- `exdqlm.vb.min_iter`: minimum iterations before convergence can trigger (default 10).
- `exdqlm.vb.patience`: number of consecutive joint-converged iterations required (default 3).
- `exdqlm.use_cpp_samplers`: use C++ samplers for `s_t`, `u_t`, `theta` (default `FALSE`). The GIG-based `u_t` sampler always uses the package C++ Devroye implementation; when `FALSE`, the remaining samplers fall back to R implementations.
- `exdqlm.use_cpp_postpred`: use C++ posterior predictive sampler (default `FALSE`).

Value

An object with classes "exdqlmISVB" and "exdqlmFit" containing the following:

- `y` - Time-series data used to fit the model.
- `run.time` - Algorithm run time in seconds.
- `iter` - Number of iterations until convergence was reached.
- `dqlm.ind` - Logical value indicating whether gamma was fixed at 0, reducing the exDQLM to the special case of the DQLM.
- `model` - List of the state-space model including GG, FF, prior parameters m_0 and C_0 .
- `p0` - The quantile which was estimated.
- `df` - Discount factors used for each block.
- `dim.df` - Dimension used for each block of discount factors.
- `sig.init` - Initial value for sigma, or value at which sigma was fixed if `fix.sigma=TRUE`.
- `seq.sigma` - Sequence of sigma estimated by the algorithm until convergence.
- `samp.theta` - Posterior sample of the state vector variational distribution.
- `samp.post.pred` - Sample of the posterior predictive distributions.
- `map.standard.forecast.errors` - MAP standardized one-step-ahead forecast errors.
- `samp.sigma` - Posterior sample of scale parameter sigma variational distribution.
- `samp.vts` - Posterior sample of latent parameters, v_t , variational distributions.
- `theta.out` - List containing the variational distribution of the state vector including filtered distribution parameters (f_m and f_C) and smoothed distribution parameters (s_m and s_C).
- `vts.out` - List containing the variational distributions of latent parameters v_t .
- `fix.sigma` Logical value indicating whether sigma was fixed at `sig.init`.
- `diagnostics` - List containing ELBO trace, standardized VB iteration trace `diagnostics$vb_trace` (iteration-wise ELBO / sigma / gamma / convergence deltas), and convergence diagnostics (joint stopping status, deltas for state/sigma/gamma/ELBO, and criteria used).

If `dqlm.ind=FALSE`, the object also contains:

- `gam.init` - Initial value for gamma, or value at which gamma was fixed if `fix.gamma=TRUE`.
- `seq.gamma` - Sequence of gamma estimated by the algorithm until convergence.
- `samp.gamma` - Posterior sample of skewness parameter gamma variational distribution.
- `samp.sts` - Posterior sample of latent parameters, s_t , variational distributions.
- `gammasig.out` - List containing the IS estimate of the variational distribution of sigma and gamma.
- `sts.out` - List containing the variational distributions of latent parameters s_t .
- `fix.gamma` Logical value indicating whether gamma was fixed at `gam.init`.

Or if `dqlm.ind=TRUE`, the object also contains:

- `sig.out` - As above but for the DQLM case ($\gamma = 0$); list containing the IS estimate of the variational distribution of sigma.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 20L)
y = scIVTmag[1:120]
trend.comp = polytrendMod(1, stats::quantile(y, 0.85), 10)
seas.comp = seasMod(365, c(1,2), C0 = 10*diag(4))
model = trend.comp + seas.comp
# Legacy ISVB fit retained for backward-compatible comparisons
M0 = exdqlmISVB(y, p0 = 0.85, model, df = c(1,1), dim.df = c(1,4),
               gam.init = -3.5, sig.init = 15, tol = 0.2,
               n.IS = 20, n.samp = 20, verbose = FALSE)
head(M0$diagnostics$vb_trace)

M0_al = exdqlmISVB(y, p0 = 0.85, model, df = c(1,1), dim.df = c(1,4),
                  dqlm.ind = TRUE, sig.init = 15, tol = 0.2,
                  n.IS = 20, n.samp = 20, verbose = FALSE)
tail(M0_al$diagnostics$vb_trace$elbo, 2)
options(old)
```

exdqlmLDVB

exDQLM - LDVB algorithm

Description

The function applies a Laplace-Delta Variational Bayes (LDVB) algorithm to estimate the posterior of an exDQLM. For unrestricted exAL fits, the default scale-skewness block uses a structured $q(\gamma)q(\sigma \mid \gamma)$ approximation. A two-dimensional Laplace-delta block is available through `vb_control$sigmagam`.

Usage

```
exdqlmLDVB(y, p0, model, df, dim.df, fix.gamma = FALSE, gam.init = NA,
           fix.sigma = FALSE, sig.init = NA, dqlm.ind = FALSE, exps0,
           tol = 0.1, n.samp = 200, PriorSigma = NULL, PriorGamma = NULL,
           vb_control = NULL, verbose = TRUE, debug_shapes = FALSE,
           debug_every = 5)
```

Arguments

<code>y</code>	A univariate time-series.
<code>p0</code>	The quantile of interest, a value between 0 and 1.
<code>model</code>	List of the state-space model including GG, FF, prior parameters <code>m0</code> and <code>C0</code> .
<code>df</code>	Discount factors for each block.
<code>dim.df</code>	Dimension of each block of discount factors.
<code>fix.gamma</code>	Logical value indicating whether to fix gamma at <code>gam.init</code> . Default is FALSE.

<code>gam.init</code>	Initial value for gamma (skewness parameter), or value at which gamma will be fixed if <code>fix.gamma=TRUE</code> .
<code>fix.sigma</code>	Logical value indicating whether to fix sigma at <code>sig.init</code> . Default is <code>FALSE</code> .
<code>sig.init</code>	Initial value for sigma (scale parameter), or value at which sigma will be fixed if <code>fix.sigma=TRUE</code> .
<code>dqlm.ind</code>	Logical value indicating whether to fix gamma at 0, reducing the exDQLM to the special case of the DQLM. Default is <code>FALSE</code> .
<code>exps0</code>	Initial value for dynamic quantile. If <code>exps0</code> is not specified, it is set to the DLM estimate of the p_0 quantile.
<code>tol</code>	Tolerance for convergence of dynamic quantile estimates. Default is <code>tol=0.1</code> .
<code>n.samp</code>	Number of samples to draw from the approximated posterior distribution. Default is <code>n.samp=200</code> .
<code>PriorSigma</code>	List of parameters for inverse gamma prior on sigma; shape <code>a_sig</code> and scale <code>b_sig</code> . Default is an inverse gamma with mean 1 (or <code>sig.init</code> if provided) and variance 10.
<code>PriorGamma</code>	List of parameters for truncated student-t prior on gamma; center <code>m_gam</code> , scale <code>s_gam</code> and degrees of freedom <code>df_gam</code> . Default is a standard student-t with 1 degree of freedom, truncated to the support of gamma.
<code>vb_control</code>	Optional normalized VB control list, usually from <code>exal_make_vb_control()</code> . When supplied, the core VB arguments and warmup blocks are read from <code>vb_control</code> first and then merged with the explicit function arguments. When omitted, exAL-style VB fits use the package's conservative default (sigma, gamma) warmup profile automatically; explicit controls remain the advanced override path.
<code>verbose</code>	Logical value indicating whether progress should be displayed.
<code>debug_shapes</code>	Logical; if <code>TRUE</code> , print KF input/output shapes every <code>debug_every</code> iterations.
<code>debug_every</code>	Integer; frequency (in iterations) for shape prints when <code>debug_shapes=TRUE</code> .

Details

Advanced options (set via `options()`):

- `exdqlm.use_cpp_kf`: use the C++ Kalman filter bridge (default `TRUE`).
- `exdqlm.compute_elbo`: compute ELBO every iteration (default `TRUE`).
- `exdqlm.tol_elbo`: ELBO convergence tolerance (default `1e-6`).
- `exdqlm.tol_sigma`: sigma-delta convergence tolerance (default: `tol`).
- `exdqlm.tol_gamma`: gamma-delta convergence tolerance (default: `tol`).
- `exdqlm.vb.min_iter`: minimum iterations before convergence can trigger (default 10).
- `exdqlm.vb.patience`: number of consecutive joint-converged iterations required (default 3).
- `exdqlm.use_cpp_samplers`: use C++ samplers for `s_t`, `u_t`, `theta` (default `FALSE`). The GIG-based `u_t` sampler always uses the package C++ Devroye implementation; when `FALSE`, the remaining samplers fall back to R implementations.
- `exdqlm.use_cpp_postpred`: use C++ posterior predictive sampler (default `FALSE`).

- `exdqlm.dynamic.ldvb.sts`: optional warmup/freeze controls for the exDQLM latent s_t VB block. Supported fields are `freeze_warmup_iters`, `force_after_warmup`, and `min_postwarmup_updates`.
- `exdqlm.dynamic.ldvb.sigmagam`: optional controls for the exAL (σ, γ) VB block. The default factorization = "structured" uses $q(\gamma)q(\sigma | \gamma)$. Use factorization = "laplace_delta" for the legacy two-dimensional transformed Gaussian factor.

Value

An object with classes "exdqlmLDVB" and "exdqlmFit" containing the following:

- `y` - Time-series data used to fit the model.
- `run.time` - Algorithm run time in seconds.
- `iter` - Number of iterations until convergence was reached.
- `dqlm.ind` - Logical value indicating whether gamma was fixed at 0, reducing the exDQLM to the special case of the DQLM.
- `model` - List of the state-space model including GG, FF, prior parameters m_0 and C_0 .
- `p0` - The quantile which was estimated.
- `df` - Discount factors used for each block.
- `dim.df` - Dimension used for each block of discount factors.
- `sig.init` - Initial value for sigma, or value at which sigma was fixed if `fix.sigma=TRUE`.
- `seq.sigma` - Sequence of sigma estimated by the algorithm until convergence.
- `samp.theta` - Posterior sample of the state vector variational distribution.
- `samp.post.pred` - Sample of the posterior predictive distributions.
- `map.standard.forecast.errors` - MAP standardized one-step-ahead forecast errors.
- `samp.sigma` - Posterior sample of scale parameter sigma variational distribution.
- `samp.vts` - Posterior sample of latent parameters, v_t , variational distributions.
- `theta.out` - List containing the variational distribution of the state vector including filtered distribution parameters (f_m and f_C) and smoothed distribution parameters (s_m and s_C).
- `vts.out` - List containing the variational distributions of latent parameters v_t .
- `fix.sigma` Logical value indicating whether sigma was fixed at `sig.init`.
- `diagnostics` - List containing ELBO trace, standardized VB iteration trace `diagnostics$vb_trace` (iteration-wise ELBO / sigma / gamma / convergence deltas), and convergence diagnostics (joint stopping status, deltas for state/sigma/gamma/ELBO, and criteria used).

If `dqlm.ind=FALSE`, the list also contains:

- `gam.init` - Initial value for gamma, or value at which gamma was fixed if `fix.gamma=TRUE`.
- `seq.gamma` - Sequence of gamma estimated by the algorithm until convergence.
- `samp.gamma` - Posterior sample of skewness parameter gamma variational distribution.
- `samp.sts` - Posterior sample of latent parameters, s_t , variational distributions.
- `gammasig.out` - List containing the variational approximation for sigma and gamma. In the default structured factor this includes the bounded-logit gamma quadrature grid and conditional GIG scale summaries; in the legacy Laplace-delta factor it includes the transformed mean and covariance.

- `sts.out` - List containing the variational distributions of latent parameters `s_t`.
- `fix.gamma` Logical value indicating whether gamma was fixed at `gam.init`.

Or if `dqlm.ind=TRUE`, the list also contains:

- `sig.out` - As above but for the DQLM case ($\gamma = 0$), the LD approximation for sigma.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 20L)
y = scIVTmag[1:80]
trend.comp = polytrendMod(1, stats::quantile(y, 0.85), 10)
seas.comp = seasMod(365, c(1,2), C0 = 10*diag(4))
model = trend.comp + seas.comp
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(1,1), dim.df = c(1,4),
               gam.init = -3.5, sig.init = 15, tol = 0.2,
               n.samp = 20, verbose = FALSE)

M0_al = exdqlmLDVB(y, p0 = 0.85, model, df = c(1,1), dim.df = c(1,4),
                  dqlm.ind = TRUE, sig.init = 15, tol = 0.2,
                  n.samp = 20, verbose = FALSE)

options(old)
```

exdqlmMCMC

exDQLM - MCMC algorithm

Description

The function applies a Markov chain Monte Carlo (MCMC) algorithm to sample the posterior of an exDQLM.

Usage

```
exdqlmMCMC(y, p0, model, df, dim.df, fix.gamma = FALSE, gam.init = NA,
           fix.sigma = FALSE, sig.init = NA, dqlm.ind = FALSE, Sig.mh,
           joint.sample = FALSE, n.burn = 2000, n.mcmc = 1500,
           init.from.isvb = FALSE, PriorSigma = NULL, PriorGamma = NULL,
           verbose = TRUE, init.from.vb = TRUE, vb_init_controls = NULL,
           vb_init_fit = NULL, mcmc_control = NULL, sigmagam_controls = NULL,
           latent_state_controls = NULL, theta_state_controls = NULL,
           dqlm_sigma_controls = NULL,
           mh.proposal = c("collapsed_slice", "slice", "laplace_rw", "rw"),
           mh.adapt = TRUE, mh.adapt.interval = 50L,
           mh.target.accept = c(0.20, 0.45), mh.scale.bounds = c(0.1, 10),
           mh.max_scale.step = 0.35, mh.min_burn_adapt = 50L,
           slice.width = 0.1, slice.max.steps = Inf, trace.diagnostics = TRUE,
           trace.every = 1L, verbose.every = 500L, progress_callback = NULL)
```

Arguments

<code>y</code>	A univariate time-series.
<code>p0</code>	The quantile of interest, a value between 0 and 1.
<code>model</code>	List of the state-space model including GG, FF, prior parameters <code>m0</code> and <code>C0</code> .
<code>df</code>	Discount factors for each block.
<code>dim.df</code>	Dimension of each block of discount factors.
<code>fix.gamma</code>	Logical value indicating whether to fix gamma at <code>gam.init</code> . Default is FALSE.
<code>gam.init</code>	Initial value for gamma (skewness parameter), or value at which gamma will be fixed if <code>fix.gamma</code> = TRUE.
<code>fix.sigma</code>	Logical value indicating whether to fix sigma at <code>sig.init</code> . Default is FALSE.
<code>sig.init</code>	Initial value for sigma (scale parameter), or value at which sigma will be fixed if <code>fix.sigma</code> = TRUE.
<code>dqlm.ind</code>	Logical value indicating whether to fix gamma at 0, reducing the exDQLM to the AL/DQLM special case. Default is FALSE.
<code>Sig.mh</code>	Covariance matrix used in the random walk MH step to jointly sample sigma and gamma.
<code>joint.sample</code>	Logical value indicating whether or not to recompute <code>Sig.mh</code> based off the initial burn-in samples of gamma and sigma. Default is FALSE.
<code>n.burn</code>	Number of MCMC iterations to burn. Default is <code>n.burn</code> = 2000.
<code>n.mcmc</code>	Number of MCMC iterations to sample. Default is <code>n.mcmc</code> = 1500.
<code>init.from.isvb</code>	Logical value indicating whether to use the legacy ISVB warm start when <code>init.from.vb</code> = TRUE. Default is FALSE, which favors LDVB as the default VB warm start. This flag only chooses the warm-start source; it does not change the subsequent MCMC proposal kernel.
<code>init.from.vb</code>	Optional logical. If TRUE, run a VB pre-initialization step (LDVB by default, or ISVB when <code>init.from.isvb</code> = TRUE) and initialize MCMC from converged VB moments. Default is TRUE. If explicitly set to NULL, it falls back to <code>init.from.isvb</code> behavior for backward compatibility.
<code>vb_init_controls</code>	Optional list controlling VB warm start. Supported keys: <code>method</code> ("isvb" or "ldvb"), <code>tol</code> , <code>n.IS</code> , <code>n.samp</code> , <code>max_iter</code> , <code>verbose</code> .
<code>vb_init_fit</code>	Optional precomputed VB fit object. If supplied, warm start uses this object directly and does not rerun VB internally.
<code>mcmc_control</code>	Optional normalized MCMC control list, usually from <code>exal_make_mcmc_control()</code> . When supplied, the core MCMC arguments and warmup blocks are read from <code>mcmc_control</code> first and then merged with the explicit function arguments. When omitted, exAL-style dynamic MCMC uses the package's conservative default (<code>sigma</code> , <code>gamma</code>) warmup profile automatically; explicit controls remain the advanced override path.
<code>sigmagam_controls</code>	Optional list controlling warmup/freeze for the exDQLM sigma/gamma block during MCMC.

latent_state_controls	Optional list controlling early latent-state warmup/freeze in dynamic MCMC. Supported keys include freeze_burnin_iters, freeze_only_during_burn, force_after_warmup, and mode ("u_only" or "u_st_pair").
theta_state_controls	Optional list controlling early theta-state warmup/freeze in dynamic MCMC. Supported keys include freeze_burnin_iters, freeze_only_during_burn, and force_after_warmup.
dqlm_sigma_controls	Optional list controlling sigma-only warmup/freeze in the DQLM branch. Supported keys mirror sigmagam_controls.
mh.proposal	Character; proposal kernel for the exDQLM scale/skew block. "collapsed_slice" (default) integrates out sigma for the bounded gamma slice step and then re-draws sigma from its exact GIG conditional. "slice" keeps the previous exact conditional sigma draw followed by bounded slice sampling directly on gamma. "laplace_rw" uses a Laplace-informed covariance then RW, and "rw" uses joint random-walk MH on (log sigma, logit gamma). This choice is separate from the VB warm-start method.
mh.adapt	Logical; adapt MH proposal scale during burn-in.
mh.adapt.interval	Integer; adaptation interval (iterations).
mh.target.accept	Numeric length-2 vector with lower/upper target acceptance rates.
mh.scale.bounds	Numeric length-2 vector with min/max global scaling for MH covariance.
mh.max_scale.step	Numeric in (0,1); maximum fractional scale change per adaptation step.
mh.min_burn_adapt	Minimum burn-in iterations required to enable adaptation.
slice.width	Positive numeric width for the bounded slice sampler when mh.proposal is "collapsed_slice" or "slice". Default 0.1 for parity with bqrgal.
slice.max.steps	Positive integer or Inf; maximum stepping-out expansions for the slice sampler.
trace.diagnostics	Logical; if TRUE, retain per-iteration sigma/gamma/s/u diagnostics under mh.diagnostics\$trace. Set FALSE for lighter-weight runs.
trace.every	Positive integer; when trace.diagnostics = TRUE, record one diagnostics row every trace.every iterations.
verbose.every	Positive integer controlling how often console progress is printed when verbose = TRUE. Default 500, independent of trace.every.
progress_callback	Optional callback invoked with a named list at MCMC start, at each progress checkpoint, and on completion. Intended for workflow-level progress logging.
PriorSigma	List of parameters for inverse gamma prior on sigma; shape a_sig and scale b_sig. Default is an inverse gamma with mean 1, or sig.init when supplied, and variance 10.

PriorGamma	List of parameters for truncated Student-t prior on gamma; center <code>m_gam</code> , scale <code>s_gam</code> , and degrees of freedom <code>df_gam</code> . Default is a standard Student-t with 1 degree of freedom, truncated to the support of gamma.
verbose	Logical value indicating whether progress should be displayed.

Value

An object with classes "exdqlmMCMC" and "exdqlmFit" containing the following:

- `y` - Time-series data used to fit the model.
- `run.time` - Algorithm run time in seconds.
- `dqlm.ind` - Logical value indicating whether gamma was fixed at 0, reducing the exDQLM to the special case of the DQLM.
- `model` - List of the state-space model including GG, FF, prior parameters m_0 and C_0 .
- `p0` - The quantile which was estimated.
- `df` - Discount factors used for each block.
- `dim.df` - Dimension used for each block of discount factors.
- `samp.theta` - Posterior sample of the state vector.
- `samp.post.pred` - Sample of the posterior predictive distributions.
- `map.standard.forecast.errors` - MAP standardized one-step-ahead forecast errors.
- `samp.sigma` - Posterior sample of scale parameter sigma.
- `samp.vts` - Posterior sample of latent parameters, v_t .
- `theta.out` - List containing the distributions of the state vector including filtered distribution parameters (f_m and f_C) and smoothed distribution parameters (s_m and s_C).
- `n.burn` - Number of MCMC iterations that were burned.
- `n.mcmc` - Number of MCMC iterations that were sampled.

If `dqlm.ind=FALSE`, the object also contains the following:

- `samp.gamma` - Posterior sample of skewness parameter gamma.
- `samp.sts` - Posterior sample of latent parameters, s_t .
- `init.log.sigma` - Burned samples of log sigma from the random walk MH joint sampling of sigma and gamma.
- `init.logit.gamma` - Burned samples of logit gamma from the random walk MH joint sampling of sigma and gamma.
- `accept.rate` - Acceptance rate of the MH step.
- `accept.rate.burn` - MH acceptance rate during burn-in.
- `accept.rate.keep` - MH acceptance rate in kept MCMC samples.
- `Sig.mh` - Covariance matrix used in MH step to jointly sample sigma and gamma.
- `mh.diagnostics` - MH tuning diagnostics (proposal mode, scaling path, adaptation summary).
- `diagnostics` - ESS and chain-ready summaries for sigma/gamma.

Examples

```

data("scIVTmag", package = "exdqlm")
y = scIVTmag[1:80]
trend.comp = polytrendMod(order = 1, m0 = stats::quantile(y, 0.85), C0 = 10)
seas.comp = seasMod(p = 365, h = c(1,2), C0 = 10*diag(4))
model = trend.comp + seas.comp
M2 = exdqlmMCMC(y, p0=0.85, model, df = c(1,1), dim.df = c(1,4),
               gam.init = -3.5, sig.init = 15,
               n.burn = 40, n.mcmc = 40,
               init.from.vb = FALSE, verbose = FALSE)

M2_al = exdqlmMCMC(y, p0=0.85, model, df = c(1,1), dim.df = c(1,4),
                  dqlm.ind = TRUE, sig.init = 15,
                  n.burn = 30, n.mcmc = 30,
                  init.from.vb = FALSE, verbose = FALSE)

```

exdqlmPlot

*Plot exDQLM***Description**

The function plots posterior mean summaries and 95% credible intervals (CrIs) of the dynamic quantile of an exDQLM.

Usage

```

exdqlmPlot(
  m1,
  add = FALSE,
  col = "purple",
  cr.percent = 0.95,
  plot = TRUE,
  xlim = NULL,
  ylim = NULL,
  xlab = "time",
  ylab = NULL,
  lwd = 1.5,
  lwd.interval = 0.75,
  lty.interval = 2
)

```

Arguments

m1 A fitted dynamic exdqlmFit object, such as an object returned by [exdqlmLDVB](#), [exdqlmMCMC](#), or legacy [exdqlmISVB](#).

add	Logical value indicating whether the dynamic quantile will be added to existing plot. Default is FALSE.
col	Character vector of length 1 giving color of the dynamic quantile to be plotted. Default is purple.
cr.percent	Numeric in (0, 1) indicating the probability mass for the credible intervals (e.g., 0.95). Default 0.95.
plot	Logical value indicating whether to draw the plot. If FALSE, the function only returns the plotted summaries. Default is TRUE.
xlim, ylim	Optional limits passed to the base plotting call when plot = TRUE.
xlab, ylab	Optional axis labels passed to the base plotting call when plot = TRUE.
lwd, lwd.interval	Line widths for the dynamic quantile and credible interval bounds, respectively.
lty.interval	Line type for the credible interval bounds.

Value

A list of the following is returned:

- map.quant - Posterior mean summary of the dynamic quantile (legacy field name retained for backward compatibility).
- lb.quant - Lower bound of the 95% CrIs of the dynamic quantile.
- ub.quant - Upper bound of the 95% CrIs of the dynamic quantile.
- x - Time/index values used for plotting.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
exdqlmPlot(M0, col = "blue")
q.summary = exdqlmPlot(M0, plot = FALSE)
options(old)
```

exdqlmTransferISVB	<i>Transfer Function exDQLM - legacy ISVB algorithm</i>
--------------------	---

Description

The function applies an Importance Sampling Variational Bayes (ISVB) algorithm to estimate the posterior of an exDQLM with exponential-decay transfer function component. This transfer wrapper is retained as a legacy path; `exdqlmTransferLDVB()` is the main VB transfer entry point.

Usage

```
exdqlmTransferISVB(
  y,
  p0,
  model,
  X,
  df,
  dim.df,
  lam,
  tf.df,
  fix.gamma = FALSE,
  gam.init = NA,
  fix.sigma = FALSE,
  sig.init = NA,
  dqlm.ind = FALSE,
  exps0,
  tol = 0.1,
  n.IS = 500,
  n.samp = 200,
  PriorSigma = NULL,
  PriorGamma = NULL,
  tf.m0 = NULL,
  tf.C0 = NULL,
  verbose = TRUE
)
```

Arguments

y	A univariate time-series.
p0	The quantile of interest, a value between 0 and 1.
model	List of the state-space model including GG, FF, prior parameters m0 and C0.
X	A numeric vector or matrix of transfer-function inputs. Vectors are treated as a univariate input series. Matrices should have one row per time point and one column per covariate.
df	Discount factors for each block.

<code>dim.df</code>	Dimension of each block of discount factors.
<code>lam</code>	Transfer function rate parameter λ , a value between 0 and 1.
<code>tf.df</code>	Discount factor specification for the transfer function component. If <code>length(tf.df) = 1</code> , the value is shared by the ζ_t state and the whole ψ_t block. If <code>length(tf.df) = 2</code> , it is interpreted as <code>c(df_zeta, df_psi_shared)</code> . If <code>length(tf.df) = k + 1</code> , where $k = ncol(X)$, the values are applied componentwise to $(\zeta_t, \psi_{1,t}, \dots, \psi_{k,t})$.
<code>fix.gamma</code>	Logical value indicating whether to fix gamma at <code>gam.init</code> . Default is FALSE.
<code>gam.init</code>	Initial value for gamma (skewness parameter), or value at which gamma will be fixed if <code>fix.gamma=TRUE</code> .
<code>fix.sigma</code>	Logical value indicating whether to fix sigma at <code>sig.init</code> . Default is FALSE.
<code>sig.init</code>	Initial value for sigma (scale parameter), or value at which sigma will be fixed if <code>fix.sigma=TRUE</code> .
<code>dqlm.ind</code>	Logical value indicating whether to fix gamma at 0, reducing the exDQLM to the special case of the DQLM. Default is FALSE.
<code>exps0</code>	Initial value for dynamic quantile. If <code>exps0</code> is not specified, it is set to the DLM estimate of the p_0 quantile.
<code>tol</code>	Tolerance for convergence of dynamic quantile estimates. Default is <code>tol=0.1</code> .
<code>n.IS</code>	Number of particles for the importance sampling of joint variational distribution of sigma and gamma. Default is <code>n.IS=500</code> .
<code>n.samp</code>	Number of samples to draw from the approximated posterior distribution. Default is <code>n.samp=200</code> .
<code>PriorSigma</code>	List of parameters for inverse gamma prior on sigma; shape <code>a_sig</code> and scale <code>b_sig</code> . Default is an inverse gamma with mean 1 (or <code>sig.init</code> if provided) and variance 10.
<code>PriorGamma</code>	List of parameters for truncated student-t prior on gamma; center <code>m_gam</code> , scale <code>s_gam</code> and degrees of freedom <code>df_gam</code> . Default is a standard student-t with 1 degree of freedom, truncated to the support of gamma.
<code>tf.m0</code>	Prior mean of the transfer function component. Defaults to a zero vector of length $k + 1$, where $k = ncol(X)$.
<code>tf.C0</code>	Prior covariance of the transfer function component. Defaults to the $(k + 1) \times (k + 1)$ identity matrix.
<code>verbose</code>	Logical value indicating whether progress should be displayed.

Details

Advanced options (set via `options()`):

- `exdqIm.use_cpp_kf`: use the C++ Kalman filter bridge (default TRUE).
- `exdqIm.compute_elbo`: compute ELBO every iteration (default TRUE).
- `exdqIm.tol_elbo`: ELBO convergence tolerance (default 1e-6).
- `exdqIm.use_cpp_samplers`: use C++ samplers for `s_t`, `u_t`, `theta` (default FALSE). The GIG-based `u_t` sampler always uses the package C++ Devroye implementation; when FALSE, the remaining samplers fall back to R implementations.
- `exdqIm.use_cpp_postpred`: use C++ posterior predictive sampler (default FALSE).

Value

An object with classes "exdqlmISVB" and "exdqlmFit" containing the following:

- `run.time` - Algorithm run time in seconds.
- `iter` - Number of iterations until convergence was reached.
- `dqlm.ind` - Logical value indicating whether gamma was fixed at 0, reducing the exDQLM to the special case of the DQLM.
- `model` - List of the augmented state-space model including GG, FF, prior parameters m_0 and C_0 .
- `p0` - The quantile which was estimated.
- `df` - Discount factors used for each block, including transfer function component.
- `dim.df` - Dimension used for each block of discount factors, including transfer function component.
- `lam` - Transfer function rate parameter lambda.
- `sig.init` - Initial value for sigma, or value at which sigma was fixed if `fix.sigma=TRUE`.
- `seq.sigma` - Sequence of sigma estimated by the algorithm until convergence.
- `samp.theta` - Posterior sample of the state vector variational distribution.
- `samp.post.pred` - Sample of the posterior predictive distributions.
- `map.standard.forecast.errors` - MAP standardized one-step-ahead forecast errors.
- `samp.sigma` - Posterior sample of scale parameter sigma variational distribution.
- `samp.vts` - Posterior sample of latent parameters, v_t , variational distributions.
- `theta.out` - List containing the variational distribution of the state vector including filtered distribution parameters (`fm` and `fC`) and smoothed distribution parameters (`sm` and `sC`).
- `vts.out` - List containing the variational distributions of latent parameters v_t .
- `median.kt` - Median number of time steps until the aggregated transfer effect $|x_t^\top \psi_{t-1}|$ is less than or equal to $1e-3$.

If `dqlm.ind=FALSE`, the object also contains:

- `gam.init` - Initial value for gamma, or value at which gamma was fixed if `fix.gamma=TRUE`.
- `seq.gamma` - Sequence of gamma estimated by the algorithm until convergence.
- `samp.gamma` - Posterior sample of skewness parameter gamma variational distribution.
- `samp.sts` - Posterior sample of latent parameters, s_t , variational distributions.
- `gamma.sig.out` - List containing the IS estimate of the variational distribution of sigma and gamma.
- `sts.out` - List containing the variational distributions of latent parameters s_t .

Or if `dqlm.ind=TRUE`, the object also contains:

- `sig.out` - As above but for the DQLM case ($\gamma = 0$); list containing the IS estimate of the variational distribution of sigma.

Examples

```
data("scIVTmag", package = "exdqIm")
data("ELIAnoms", package = "exdqIm")
old = options(exdqIm.max_iter = 20L)
y = scIVTmag[1:120]
X = ELIAnoms[1:120]
trend.comp = polytrendMod(1, stats::quantile(y, 0.85), 10)
seas.comp = seasMod(365, c(1,2), C0 = 10*diag(4))
model = trend.comp + seas.comp
# Legacy ISVB transfer fit retained for backward-compatible comparisons
M1 = exdqImTransferISVB(y, p0 = 0.85, model = model,
                        X, df = c(1,1), dim.df = c(1,4),
                        gam.init = -3.5, sig.init = 15,
                        lam = 0.38, tf.df = c(0.97,0.97),
                        n.IS = 20, n.samp = 20, tol = 0.2,
                        verbose = FALSE)
X_multi = cbind(ELIAnoms[1:120], scale(scIVTmag[1:120])[, 1])
M2 = exdqImTransferISVB(y, p0 = 0.85, model = model,
                        X_multi, df = c(1,1), dim.df = c(1,4),
                        gam.init = -3.5, sig.init = 15,
                        lam = 0.38, tf.df = c(0.97, 0.99),
                        n.IS = 20, n.samp = 20, tol = 0.2,
                        verbose = FALSE)

options(old)
```

exdqImTransferLDVB

Transfer Function exDQLM - LDVB algorithm

Description

The function applies a Laplace-Delta Variational Bayes (LDVB) algorithm to estimate the posterior of an exDQLM with an exponential-decay transfer function component. For multivariate transfer inputs, each column of X has its own instantaneous coefficient state in ψ_t , while a single scalar decay rate λ controls persistence of the accumulated transfer effect ζ_t .

Usage

```
exdqImTransferLDVB(
  y,
  p0,
  model,
  X,
  df,
  dim.df,
  lam,
  tf.df,
```

```

    fix.gamma = FALSE,
    gam.init = NA,
    fix.sigma = FALSE,
    sig.init = NA,
    dqlm.ind = FALSE,
    exps0,
    tol = 0.1,
    n.samp = 200,
    PriorSigma = NULL,
    PriorGamma = NULL,
    tf.m0 = NULL,
    tf.C0 = NULL,
    vb_control = NULL,
    verbose = TRUE,
    debug_shapes = FALSE,
    debug_every = 5
)

```

Arguments

y	A univariate time-series.
p0	The quantile of interest, a value between 0 and 1.
model	List of the state-space model including GG, FF, prior parameters m0 and C0.
X	A numeric vector or matrix of transfer-function inputs. Vectors are treated as a univariate input series. Matrices should have one row per time point and one column per covariate.
df	Discount factors for each block.
dim.df	Dimension of each block of discount factors.
lam	Single transfer-function decay-rate parameter λ , a value between 0 and 1. This scalar is shared across all transfer inputs and controls propagation of the accumulated transfer effect ζ_t .
tf.df	Discount factor specification for the transfer function component. These discount factors control the evolution variances of the transfer states, separately from the deterministic decay rate lam. If <code>length(tf.df) = 1</code> , the value is shared by the ζ_t state and the whole ψ_t block. If <code>length(tf.df) = 2</code> , it is interpreted as <code>c(df_zeta, df_psi_shared)</code> . If <code>length(tf.df) = k + 1</code> , where $k = \text{ncol}(X)$, the values are applied componentwise to $(\zeta_t, \psi_{1,t}, \dots, \psi_{k,t})$.
fix.gamma	Logical value indicating whether to fix gamma at gam.init. Default is FALSE.
gam.init	Initial value for gamma (skewness parameter), or value at which gamma will be fixed if fix.gamma=TRUE.
fix.sigma	Logical value indicating whether to fix sigma at sig.init. Default is FALSE.
sig.init	Initial value for sigma (scale parameter), or value at which sigma will be fixed if fix.sigma=TRUE.
dqlm.ind	Logical value indicating whether to fix gamma at 0, reducing the exDQLM to the special case of the DQLM. Default is FALSE.

<code>exps0</code>	Initial value for dynamic quantile. If <code>exps0</code> is not specified, it is set to the DLM estimate of the p_0 quantile.
<code>tol</code>	Tolerance for convergence of dynamic quantile estimates. Default is <code>tol=0.1</code> .
<code>n.samp</code>	Number of samples to draw from the approximated posterior distribution. Default is <code>n.samp=200</code> .
<code>PriorSigma</code>	List of parameters for inverse gamma prior on sigma; shape <code>a_sig</code> and scale <code>b_sig</code> . Default is an inverse gamma with mean 1 (or <code>sig.init</code> if provided) and variance 10.
<code>PriorGamma</code>	List of parameters for truncated student-t prior on gamma; center <code>m_gam</code> , scale <code>s_gam</code> and degrees of freedom <code>df_gam</code> . Default is a standard student-t with 1 degree of freedom, truncated to the support of gamma.
<code>tf.m0</code>	Prior mean of the transfer function component. Defaults to a zero vector of length $k + 1$, where $k = ncol(X)$.
<code>tf.C0</code>	Prior covariance of the transfer function component. Defaults to the $(k + 1) \times (k + 1)$ identity matrix.
<code>vb_control</code>	Optional normalized VB control list passed to exdq1mLDVB . Use this to set common VB controls such as <code>max_iter</code> , <code>tol</code> , or warmup blocks for the transfer-augmented LDVB fit.
<code>verbose</code>	Logical value indicating whether progress should be displayed.
<code>debug_shapes</code>	Logical; if TRUE, print KF input/output shapes every <code>debug_every</code> iterations.
<code>debug_every</code>	Integer; frequency (in iterations) for shape prints when <code>debug_shapes=TRUE</code> .

Value

An object with classes "exdq1mLDVB" and "exdq1mFit" containing the following:

- `y` - Time-series data used to fit the model.
- `run.time` - Algorithm run time in seconds.
- `iter` - Number of iterations until convergence was reached.
- `dqlm.ind` - Logical value indicating whether gamma was fixed at 0, reducing the exDQLM to the special case of the DQLM.
- `model` - List of the state-space model including GG, FF, prior parameters `m0` and `C0`.
- `p0` - The quantile which was estimated.
- `df` - Discount factors used for each block.
- `dim.df` - Dimension used for each block of discount factors.
- `sig.init` - Initial value for sigma, or value at which sigma was fixed if `fix.sigma=TRUE`.
- `seq.sigma` - Sequence of sigma estimated by the algorithm until convergence.
- `samp.theta` - Posterior sample of the state vector variational distribution.
- `samp.post.pred` - Sample of the posterior predictive distributions.
- `map.standard.forecast.errors` - MAP standardized one-step-ahead forecast errors.
- `samp.sigma` - Posterior sample of scale parameter sigma variational distribution.
- `samp.vts` - Posterior sample of latent parameters, `v_t`, variational distributions.

- `theta.out` - List containing the variational distribution of the state vector including filtered distribution parameters (`fm` and `fc`) and smoothed distribution parameters (`sm` and `sc`).
- `vt.s.out` - List containing the variational distributions of latent parameters `v_t`.
- `fix.sigma` Logical value indicating whether sigma was fixed at `sig.init`.
- `diagnostics` - List containing ELBO trace, standardized VB iteration trace `diagnostics$vb_trace` (iteration-wise ELBO / sigma / gamma / convergence deltas), and convergence diagnostics (joint stopping status, deltas for state/sigma/gamma/ELBO, and criteria used).

If `dqlm.ind=FALSE`, the list also contains:

- `gam.init` - Initial value for gamma, or value at which gamma was fixed if `fix.gamma=TRUE`.
- `seq.gamma` - Sequence of gamma estimated by the algorithm until convergence.
- `samp.gamma` - Posterior sample of skewness parameter gamma variational distribution.
- `samp.sts` - Posterior sample of latent parameters, `s_t`, variational distributions.
- `gammasig.out` - List containing the variational approximation for sigma and gamma. In the default structured factor this includes the bounded-logit gamma quadrature grid and conditional GIG scale summaries; in the legacy Laplace-delta factor it includes the transformed mean and covariance.
- `sts.out` - List containing the variational distributions of latent parameters `s_t`.
- `fix.gamma` Logical value indicating whether gamma was fixed at `gam.init`.

Or if `dqlm.ind=TRUE`, the list also contains:

- `sig.out` - As above but for the DQLM case ($\gamma = 0$), the LD approximation for sigma.

Transfer-function return fields

In addition to the standard `exdqlmLDVB()` return values, the returned `model`, `df`, and `dim.df` entries correspond to the transfer-function-augmented state-space model, with appended ζ_t and ψ_t states. The object also contains:

- `lam` - Single transfer-function decay-rate parameter λ .
- `median.kt` - Median number of time steps until the aggregated transfer effect $|x_t^\top \psi_{t-1}|$ is less than or equal to $1e-3$.
- `transfer_input_names` - Column names of the transfer inputs after normalization of `X`.

Examples

```
data("scIVTmag", package = "exdqlm")
data("ELIanom", package = "exdqlm")
old = options(exdqlm.max_iter = 20L)
y = scIVTmag[1:120]
X = ELIanom[1:120]
trend.comp = polytrendMod(1, stats::quantile(y, 0.85), 10)
seas.comp = seasMod(365, c(1,2), C0 = 10*diag(4))
model = trend.comp + seas.comp
M1 = exdqlmTransferLDVB(
  y, p0 = 0.85, model = model, X = X,
```

```

    df = c(1,1), dim.df = c(1,4),
    gam.init = -3.5, sig.init = 15,
    lam = 0.38, tf.df = c(0.97,0.97),
    n.samp = 20, tol = 0.2, vb_control = list(max_iter = 20L),
    verbose = FALSE
  )
  X_multi = cbind(ELIanom[1:120], scale(scIVTmag[1:120]))[, 1]
  M2 = exdqImTransferLDVB(
    y, p0 = 0.85, model = model, X = X_multi,
    df = c(1,1), dim.df = c(1,4),
    gam.init = -3.5, sig.init = 15,
    lam = 0.38, tf.df = c(0.97, 0.99),
    n.samp = 20, tol = 0.2, vb_control = list(max_iter = 20L),
    verbose = FALSE
  )
  options(old)

```

exdqImTransferMCMC *Transfer Function exDQLM - MCMC algorithm*

Description

The function applies a Markov chain Monte Carlo (MCMC) algorithm to sample the posterior of an exDQLM with an exponential-decay transfer function component for a fixed transfer rate parameter λ . For multivariate transfer inputs, each column of X has its own instantaneous coefficient state in ψ_t , while a single scalar decay rate λ controls persistence of the accumulated transfer effect ζ_t .

Usage

```

exdqImTransferMCMC(
  y,
  p0,
  model,
  X,
  df,
  dim.df,
  lam,
  tf.df,
  fix.gamma = FALSE,
  gam.init = NA,
  fix.sigma = FALSE,
  sig.init = NA,
  dqIm.ind = FALSE,
  Sig.mh,
  joint.sample = FALSE,
  n.burn = 2000,
  n.mcmc = 1500,

```

```

init.from.isvb = FALSE,
PriorSigma = NULL,
PriorGamma = NULL,
verbose = TRUE,
init.from.vb = TRUE,
vb_init_controls = NULL,
vb_init_fit = NULL,
mh.proposal = c("collapsed_slice", "slice", "laplace_rw", "rw"),
mh.adapt = TRUE,
mh.adapt.interval = 50L,
mh.target.accept = c(0.2, 0.45),
mh.scale.bounds = c(0.1, 10),
mh.max_scale.step = 0.35,
mh.min_burn_adapt = 50L,
slice.width = 0.1,
slice.max.steps = Inf,
trace.diagnostics = TRUE,
trace.every = 1L,
verbose.every = 500L,
progress_callback = NULL,
tf.m0 = NULL,
tf.C0 = NULL
)

```

Arguments

<code>y</code>	A univariate time-series.
<code>p0</code>	The quantile of interest, a value between 0 and 1.
<code>model</code>	List of the state-space model including GG, FF, prior parameters <code>m0</code> and <code>C0</code> .
<code>X</code>	A numeric vector or matrix of transfer-function inputs. Vectors are treated as a univariate input series. Matrices should have one row per time point and one column per covariate.
<code>df</code>	Discount factors for each block.
<code>dim.df</code>	Dimension of each block of discount factors.
<code>lam</code>	Single transfer-function decay-rate parameter λ , a value between 0 and 1. This scalar is shared across all transfer inputs and controls propagation of the accumulated transfer effect ζ_t .
<code>tf.df</code>	Discount factor specification for the transfer function component. These discount factors control the evolution variances of the transfer states, separately from the deterministic decay rate <code>lam</code> . If <code>length(tf.df) = 1</code> , the value is shared by the ζ_t state and the whole ψ_t block. If <code>length(tf.df) = 2</code> , it is interpreted as <code>c(df_zeta, df_psi_shared)</code> . If <code>length(tf.df) = k + 1</code> , where $k = ncol(X)$, the values are applied componentwise to $(\zeta_t, \psi_{1,t}, \dots, \psi_{k,t})$.
<code>fix.gamma</code>	Logical value indicating whether to fix gamma at <code>gam.init</code> . Default is FALSE.
<code>gam.init</code>	Initial value for gamma (skewness parameter), or value at which gamma will be fixed if <code>fix.gamma = TRUE</code> .

<code>fix.sigma</code>	Logical value indicating whether to fix sigma at <code>sig.init</code> . Default is FALSE.
<code>sig.init</code>	Initial value for sigma (scale parameter), or value at which sigma will be fixed if <code>fix.sigma = TRUE</code> .
<code>dqlm.ind</code>	Logical value indicating whether to fix gamma at 0, reducing the exDQLM to the AL/DQLM special case. Default is FALSE.
<code>Sig.mh</code>	Covariance matrix used in the random walk MH step to jointly sample sigma and gamma.
<code>joint.sample</code>	Logical value indicating whether or not to recompute <code>Sig.mh</code> based off the initial burn-in samples of gamma and sigma. Default is FALSE.
<code>n.burn</code>	Number of MCMC iterations to burn. Default is <code>n.burn = 2000</code> .
<code>n.mcmc</code>	Number of MCMC iterations to sample. Default is <code>n.mcmc = 1500</code> .
<code>init.from.isvb</code>	Logical value indicating whether to use the legacy ISVB warm start when <code>init.from.vb = TRUE</code> . Default is FALSE, which favors LDVB as the default VB warm start. This flag only chooses the warm-start source; it does not change the subsequent MCMC proposal kernel.
<code>PriorSigma</code>	List of parameters for inverse gamma prior on sigma; shape <code>a_sig</code> and scale <code>b_sig</code> . Default is an inverse gamma with mean 1, or <code>sig.init</code> when supplied, and variance 10.
<code>PriorGamma</code>	List of parameters for truncated Student-t prior on gamma; center <code>m_gam</code> , scale <code>s_gam</code> , and degrees of freedom <code>df_gam</code> . Default is a standard Student-t with 1 degree of freedom, truncated to the support of gamma.
<code>verbose</code>	Logical value indicating whether progress should be displayed.
<code>init.from.vb</code>	Optional logical. If TRUE, run a VB pre-initialization step (LDVB by default, or ISVB when <code>init.from.isvb = TRUE</code>) and initialize MCMC from converged VB moments. Default is TRUE. If explicitly set to NULL, it falls back to <code>init.from.isvb</code> behavior for backward compatibility.
<code>vb_init_controls</code>	Optional list controlling VB warm start. Supported keys: <code>method</code> ("isvb" or "ldvb"), <code>tol</code> , <code>n.IS</code> , <code>n.samp</code> , <code>max_iter</code> , <code>verbose</code> .
<code>vb_init_fit</code>	Optional precomputed VB fit object. If supplied, warm start uses this object directly and does not rerun VB internally.
<code>mh.proposal</code>	Character; proposal kernel for the exDQLM scale/skew block. "collapsed_slice" (default) integrates out sigma for the bounded gamma slice step and then re-draws sigma from its exact GIG conditional. "slice" keeps the previous exact conditional sigma draw followed by bounded slice sampling directly on gamma. "laplace_rw" uses a Laplace-informed covariance then RW, and "rw" uses joint random-walk MH on (log sigma, logit gamma). This choice is separate from the VB warm-start method.
<code>mh.adapt</code>	Logical; adapt MH proposal scale during burn-in.
<code>mh.adapt.interval</code>	Integer; adaptation interval (iterations).
<code>mh.target.accept</code>	Numeric length-2 vector with lower/upper target acceptance rates.

<code>mh.scale.bounds</code>	Numeric length-2 vector with min/max global scaling for MH covariance.
<code>mh.max_scale.step</code>	Numeric in (0,1); maximum fractional scale change per adaptation step.
<code>mh.min_burn_adapt</code>	Minimum burn-in iterations required to enable adaptation.
<code>slice.width</code>	Positive numeric width for the bounded slice sampler when <code>mh.proposal</code> is "collapsed_slice" or "slice". Default 0.1 for parity with bqrGal.
<code>slice.max.steps</code>	Positive integer or Inf; maximum stepping-out expansions for the slice sampler.
<code>trace.diagnostics</code>	Logical; if TRUE, retain per-iteration sigma/gamma/s/u diagnostics under <code>mh.diagnostics\$trace</code> . Set FALSE for lighter-weight runs.
<code>trace.every</code>	Positive integer; when <code>trace.diagnostics = TRUE</code> , record one diagnostics row every <code>trace.every</code> iterations.
<code>verbose.every</code>	Positive integer controlling how often console progress is printed when <code>verbose = TRUE</code> . Default 500, independent of <code>trace.every</code> .
<code>progress_callback</code>	Optional callback invoked with a named list at MCMC start, at each progress checkpoint, and on completion. Intended for workflow-level progress logging.
<code>tf.m0</code>	Prior mean of the transfer function component. Defaults to a zero vector of length $k + 1$, where $k = ncol(X)$.
<code>tf.C0</code>	Prior covariance of the transfer function component. Defaults to the $(k + 1) \times (k + 1)$ identity matrix.

Value

An object with classes "exdqImMCMC" and "exdqImFit" containing the following:

- `y` - Time-series data used to fit the model.
- `run.time` - Algorithm run time in seconds.
- `dqlm.ind` - Logical value indicating whether gamma was fixed at 0, reducing the exDQLM to the special case of the DQLM.
- `model` - List of the state-space model including GG, FF, prior parameters `m0` and `C0`.
- `p0` - The quantile which was estimated.
- `df` - Discount factors used for each block.
- `dim.df` - Dimension used for each block of discount factors.
- `samp.theta` - Posterior sample of the state vector.
- `samp.post.pred` - Sample of the posterior predictive distributions.
- `map.standard.forecast.errors` - MAP standardized one-step-ahead forecast errors.
- `samp.sigma` - Posterior sample of scale parameter sigma.
- `samp.vts` - Posterior sample of latent parameters, `v_t`.

- `theta.out` - List containing the distributions of the state vector including filtered distribution parameters (`fm` and `fC`) and smoothed distribution parameters (`sm` and `sC`).
- `n.burn` Number of MCMC iterations that were burned.
- `n.mcmc` Number of MCMC iterations that were sampled.

If `dqlm.ind=FALSE`, the object also contains the following:

- `samp.gamma` - Posterior sample of skewness parameter `gamma`.
- `samp.sts` - Posterior sample of latent parameters, `s_t`.
- `init.log.sigma` - Burned samples of log sigma from the random walk MH joint sampling of sigma and gamma.
- `init.logit.gamma` - Burned samples of logit gamma from the random walk MH joint sampling of sigma and gamma.
- `accept.rate` - Acceptance rate of the MH step.
- `accept.rate.burn` - MH acceptance rate during burn-in.
- `accept.rate.keep` - MH acceptance rate in kept MCMC samples.
- `Sig.mh` - Covariance matrix used in MH step to jointly sample sigma and gamma.
- `mh.diagnostics` - MH tuning diagnostics (proposal mode, scaling path, adaptation summary).
- `diagnostics` - ESS and chain-ready summaries for sigma/gamma.

Transfer-function return fields

In addition to the standard `exdqlmMCMC()` return values, the returned `model`, `df`, and `dim.df` entries correspond to the transfer-function-augmented state-space model, with appended ζ_t and ψ_t states. The object also contains:

- `lam` - Single transfer-function decay-rate parameter λ .
- `median.kt` - Median number of time steps until the aggregated transfer effect $|x_t^\top \psi_{t-1}|$ is less than or equal to $1e-3$.
- `transfer_input_names` - Column names of the transfer inputs after normalization of X .

Examples

```
data("scIVTmag", package = "exdqlm")
data("ELIAnoms", package = "exdqlm")
y = scIVTmag[1:120]
X = ELIAnoms[1:120]
trend.comp = polytrendMod(1, stats::quantile(y, 0.85), 10)
seas.comp = seasMod(365, c(1,2), C0 = 10*diag(4))
model = trend.comp + seas.comp
M1 = exdqlmTransferMCMC(
  y, p0 = 0.85, model = model, X = X,
  df = c(1,1), dim.df = c(1,4),
  gam.init = -3.5, sig.init = 15,
  lam = 0.38, tf.df = c(0.97,0.97),
  n.burn = 40, n.mcmc = 40,
```

```

    init.from.vb = FALSE, verbose = FALSE
  )
  X_multi = cbind(ELIAnoms[1:120], scale(scIVTmag[1:120])[, 1])
  M2 = exdqlmTransferMCMC(
    y, p0 = 0.85, model = model, X = X_multi,
    df = c(1,1), dim.df = c(1,4),
    gam.init = -3.5, sig.init = 15,
    lam = 0.38, tf.df = c(0.97, 0.99),
    n.burn = 40, n.mcmc = 40,
    init.from.vb = FALSE, verbose = FALSE
  )

```

get_gamma_bounds

*Bounds for the exAL shape parameter gamma***Description**

Returns valid lower/upper bounds (L, U) for the shape parameter gamma of the standardized extended Asymmetric Laplace (exAL), given p0 in (0,1).

Usage

```
get_gamma_bounds(p0)
```

Arguments

p0 Numeric scalar in (0, 1); typically the target quantile level.

Details

This is a user-facing convenience wrapper around the C++ routine `get_gamma_bounds_cpp()`, which performs the actual computation.

Value

A numeric vector of length 2 named `c("L", "U")`.

Examples

```

get_gamma_bounds(0.5)
get_gamma_bounds(0.9)

```

```
is.exalStaticDiagnostic
      exalStaticDiagnostic objects
```

Description

is.exalStaticDiagnostic tests if its argument is an exalStaticDiagnostic object.

Usage

```
is.exalStaticDiagnostic(x)
```

Arguments

x an **R** object

```
is.exalStaticFit        exalStaticFit objects
```

Description

is.exalStaticFit tests if its argument is a fitted static exAL regression object, including MCMC and LDVB fits.

Usage

```
is.exalStaticFit(m)
```

Arguments

m an **R** object

```
is.exalStaticLDVB      exalStaticLDVB objects
```

Description

is.exalStaticLDVB tests if its argument is an exalStaticLDVB object.

Usage

```
is.exalStaticLDVB(m)
```

Arguments

m an **R** object

is.exalStaticMCMC	exalStaticMCMC <i>objects</i>
-------------------	-------------------------------

Description

is.exalStaticMCMC tests if its argument is an exalStaticMCMC object.

Usage

```
is.exalStaticMCMC(m)
```

Arguments

m an **R** object

is.exdqlm	exdqlm <i>objects</i>
-----------	-----------------------

Description

is.exdqlm tests if its argument is a exdqlm object.

Usage

```
is.exdqlm(m)
```

Arguments

m an **R** object

is.exdqlmDiagnostic	exdqlmDiagnostic <i>objects</i>
---------------------	---------------------------------

Description

is.exdqlmDiagnostic tests if its argument is a exdqlmDiagnostic object.

Usage

```
is.exdqlmDiagnostic(x)
```

Arguments

x an **R** object

is.exdqlmFit	exdqlmFit <i>objects</i>
--------------	--------------------------

Description

is.exdqlmFit tests if its argument is a fitted dynamic exdqlm object, including MCMC, LDVB, and legacy ISVB fits.

Usage

```
is.exdqlmFit(m)
```

Arguments

m	an R object
---	--------------------

is.exdqlmForecast	exdqlmForecast <i>objects</i>
-------------------	-------------------------------

Description

is.exdqlmForecast tests if its argument is a exdqlmForecast object.

Usage

```
is.exdqlmForecast(x)
```

Arguments

x	an R object
---	--------------------

is.exdqlmForecastDiagnostic	exdqlmForecastDiagnostic <i>objects</i>
-----------------------------	---

Description

is.exdqlmForecastDiagnostic tests if its argument is an exdqlmForecastDiagnostic object.

Usage

```
is.exdqlmForecastDiagnostic(x)
```

Arguments

x	an R object.
---	---------------------

is.exdqlmISVB	exdqlmISVB <i>objects</i>
---------------	---------------------------

Description

is.exdqlmISVB tests if its argument is a exdqlmISVB object.

Usage

```
is.exdqlmISVB(m)
```

Arguments

m an **R** object

is.exdqlmLDVB	exdqlmLDVB <i>objects</i>
---------------	---------------------------

Description

is.exdqlmLDVB tests if its argument is a exdqlmLDVB object.

Usage

```
is.exdqlmLDVB(m)
```

Arguments

m an **R** object

is.exdqlmMCMC	exdqlmMCMC <i>objects</i>
---------------	---------------------------

Description

is.exdqlmMCMC tests if its argument is a exdqlmMCMC object.

Usage

```
is.exdqlmMCMC(m)
```

Arguments

m an **R** object

is.exdqlmSynthesis	exdqlmSynthesis objects
--------------------	-------------------------

Description

is.exdqlmSynthesis tests if its argument is an exdqlmSynthesis object returned by [quantileSynthesis](#).

Usage

```
is.exdqlmSynthesis(x)
```

Arguments

x	an R object
---	--------------------

pexal	<i>Cumulative Distribution Function (CDF) for the exAL Distribution</i>
-------	---

Description

Vectorized over q.

Usage

```
pexal(
  q,
  p0 = 0.5,
  mu = 0,
  sigma = 1,
  gamma = 0,
  lower.tail = TRUE,
  log.p = FALSE
)
```

Arguments

q	Numeric vector of quantiles.
p0	Probability level used in the quantile parametrization. Scalar in (0, 1). Default 0.5.
mu	Location parameter (scalar). Default 0.
sigma	Scale parameter (scalar, strictly positive). Default 1.
gamma	Skewness parameter controlling asymmetry (scalar). Must be within valid bounds implied by p0. Default 0.
lower.tail	Logical scalar; if TRUE (default) return $P(X \leq q)$, otherwise $P(X > q)$.
log.p	Logical scalar; if TRUE, return log-probabilities.

Value

Numeric vector of CDF values (same length as q).

Examples

```
pexal(0)
pexal(c(-1, 0, 1), p0 = 0.5, mu = 0, sigma = 1, gamma = 0.1)
```

```
plot.exalStaticDiagnostic
```

Plot Method for exalStaticDiagnostic Objects

Description

Plot fitted-quantile diagnostics or posterior coefficient intervals from a static diagnostic object. The "quantile" display shows fitted conditional quantiles for one or two static fits, together with optional observed responses and a reference quantile curve. The "coefficients" display shows posterior coefficient intervals and can optionally overlay known coefficient values in simulation studies.

Usage

```
## S3 method for class 'exalStaticDiagnostic'
plot(
  x,
  cols = c("red", "blue"),
  type = c("quantile", "coefficients"),
  beta.ref = NULL,
  include.intercept = TRUE,
  coef.names = NULL,
  xlab = NULL,
  ylab = NULL,
  ylim = NULL,
  legend.labels = NULL,
  beta.ref.label = "reference",
  legend = TRUE,
  ...
)
```

Arguments

x	An exalStaticDiagnostic object.
cols	Character vector of length 1 or 2 giving color(s) used to plot diagnostics.
type	Character string; "quantile" plots fitted conditional quantile summaries, and "coefficients" plots posterior coefficient intervals.

beta.ref	Optional coefficient reference vector for type = "coefficients". This is typically available only in simulation benchmarks. It is used as a plotting overlay, not as a package diagnostic metric.
include.intercept	Logical; if FALSE, omit the first coefficient from type = "coefficients" plots.
coef.names	Optional names for coefficients in type = "coefficients" plots.
xlab, ylab	Optional axis labels.
ylim	Optional y-axis limits.
legend.labels	Optional labels for the first and second model intervals in type = "coefficients" plots.
beta.ref.label	Label for the optional beta.ref overlay.
legend	Logical; if TRUE, add a legend to coefficient plots.
...	Additional arguments passed to plotting functions.

plot.exalStaticFit *Plot Method for exalStaticFit Objects*

Description

Plot fitted conditional quantile summaries from a static AL/exAL regression fit. The method works for objects returned by `exalStaticLDVB` and `exalStaticMCMC` through their shared `exalStaticFit` family class.

Usage

```
## S3 method for class 'exalStaticFit'
plot(x, X = NULL, add = FALSE, col = "purple", cr.percent = 0.95, ...)
```

Arguments

x	A fitted static <code>exalStaticFit</code> object.
X	Optional design matrix used to compute fitted quantiles. If omitted, the method uses <code>x\$X</code> when available.
add	Logical; add to an existing plot.
col	Character vector of length 1 giving color for fitted quantiles.
cr.percent	Numeric in (0, 1) for credible-interval mass.
...	Additional arguments passed to <code>plot</code> when <code>add = FALSE</code> .

Value

Invisibly returns a list with `map.quant` (legacy field name for fitted posterior mean quantiles), `lb.quant`, and `ub.quant`.

plot.exalStaticLDVB *Plot Method for exalStaticLDVB Objects*

Description

Plot Method for exalStaticLDVB Objects

Usage

```
## S3 method for class 'exalStaticLDVB'
plot(x, X = NULL, add = FALSE, col = "purple", cr.percent = 0.95, ...)
```

Arguments

x	An exalStaticLDVB object.
X	Optional design matrix used to compute fitted quantiles. If omitted, the method uses x\$X when available.
add	Logical; add to an existing plot.
col	Character vector of length 1 giving color for fitted quantiles.
cr.percent	Numeric in (0, 1) for credible-interval mass.
...	Additional arguments passed to plot when add = FALSE.

Value

A list with map.quant (legacy field name for fitted posterior mean quantiles), lb.quant, and ub.quant.

plot.exalStaticMCMC *Plot Method for exalStaticMCMC Objects*

Description

Plot Method for exalStaticMCMC Objects

Usage

```
## S3 method for class 'exalStaticMCMC'
plot(x, X = NULL, add = FALSE, col = "purple", cr.percent = 0.95, ...)
```

Arguments

x	An exalStaticMCMC object.
X	Optional design matrix used to compute fitted quantiles. If omitted, the method uses x\$X when available.
add	Logical; add to an existing plot.
col	Character vector of length 1 giving color for fitted quantiles.
cr.percent	Numeric in (0, 1) for credible-interval mass.
...	Additional arguments passed to plot when add = FALSE.

Value

A list with map.quant (legacy field name for fitted posterior mean quantiles), lb.quant, and ub.quant.

plot.exdqlmDiagnostic *Plot Method for exdqlmDiagnostic Objects*

Description

This function produces the QQ plot and ACF plot corresponding to the one-step-ahead distribution sequence, together with a time series plot of the MAP standard forecast errors.

Usage

```
## S3 method for class 'exdqlmDiagnostic'
plot(x, ...)
```

Arguments

x	An exdqlmDiagnostic object.
...	Additional graphical arguments. The optional cols element controls the colors used for the first and second model when comparing two fits.

Value

Invisibly returns x.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.95), dim.df = c(1),
  gam.init = -3.5, sig.init = 15,
  n.samp = 20, tol = 0.2, verbose = FALSE)
```

```
M0.diags = diagnostics(M0)
plot(M0.diags)
options(old)
```

plot.exdqlmFit

Plot Method for Dynamic exdqlmFit Objects

Description

Plot fitted dynamic quantiles, fitted component contributions, or individual state elements from a dynamic fit. The default type = "quantile" plots posterior mean summaries and 95% credible intervals (CrIs) of the dynamic quantile. type = "component" plots posterior mean summaries and CrIs for a specified component. type = "state" plots posterior mean summaries and CrIs of a single element of the dynamic state vector.

Usage

```
## S3 method for class 'exdqlmFit'
plot(
  x,
  type = c("quantile", "component", "state"),
  index = NULL,
  add = FALSE,
  col = "purple",
  cr.percent = 0.95,
  xlim = NULL,
  ylim = NULL,
  xlab = "time",
  ylab = NULL,
  lwd = 1.5,
  lwd.interval = 0.75,
  lty.interval = 2,
  ...
)
```

Arguments

x	A fitted dynamic exdqlmFit object.
type	Character string specifying the plot type. Use "quantile" for the fitted dynamic quantile, "component" for the contribution of a block of state elements, or "state" for a single state element.
index	Required for type = "component" or type = "state". For type = "state", index must have length 1 indicating a single element of the state vector to be plotted. For type = "component", index should be consecutive state indices in $\{1, \dots, q\}$ indicating the component to be plotted.

add	Optional logical value indicating whether the estimate will be added to existing plot. Default is FALSE.
col	Optional character vector of length 1 giving color of the estimate to be plotted. Default is purple.
cr.percent	Optional numeric in (0, 1) indicating the probability mass for the credible intervals (e.g., 0.95). Default 0.95.
xlim, ylim	Optional limits passed to the base plotting call.
xlab, ylab	Optional axis labels passed to the base plotting call.
lwd, lwd.interval	Line widths for the estimate and credible interval bounds, respectively.
lty.interval	Line type for the credible interval bounds.
...	Additional arguments.

Value

Invisibly returns a list of the following:

- map.quant - Posterior mean summary of the dynamic estimate (legacy field name retained for backward compatibility).
- lb.quant - Lower bound of the 95% CrIs of the dynamic estimate.
- ub.quant - Upper bound of the 95% CrIs of the dynamic estimate.
- x - Time/index values used for plotting.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:80]
trend.comp = polytrendMod(2, rep(mean(y), 2), 10*diag(2))
seas.comp = seasMod(365, c(1, 2), C0 = 10*diag(4))
model = trend.comp + seas.comp
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.98, 1), dim.df = c(2, 4),
               gam.init = -3.5, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)

# plot quantile
plot(M0)
# plot first harmonic component
plot(M0, type="component", index = c(3, 4), col = "blue")
options(old)
```

plot.exdqlmForecast *Plot Method for exdqlmForecast Objects*

Description

Plot filtered and forecast quantiles with equal-tailed credible intervals.

Usage

```
## S3 method for class 'exdqlmForecast'
plot(x, ...)
```

Arguments

x An exdqlmForecast object.

... Additional graphical arguments. The optional cols element controls fitted/forecast colors, and add controls whether the forecast is added to an existing plot.

Value

Invisibly returns x.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
                dqlm.ind = TRUE, sig.init = 15,
                n.samp = 20, tol = 0.2, verbose = FALSE)
M0.forecast = predict(M0, start.t = 50, k = 5)
plot(M0.forecast)
options(old)
```

plot.exdqlmISVB *Plot Method for exdqlmISVB Objects*

Description

Plot Method for exdqlmISVB Objects

Usage

```
## S3 method for class 'exdqlmISVB'
plot(x, type = c("quantile", "component", "state"), index = NULL, ...)
```

Arguments

x	An exdqlmISVB object.
type	Character string specifying "quantile", "component", or "state".
index	Required for type = "component" or type = "state".
...	Additional arguments.

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
# Legacy ISVB object retained for backward-compatible plotting methods
M0 = exdqlmISVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.IS = 20, n.samp = 20, tol = 0.2,
               verbose = FALSE)

plot(M0)
options(old)
```

plot.exdqlmLDVB

Plot Method for exdqlmLDVB Objects

Description

Plot Method for exdqlmLDVB Objects

Usage

```
## S3 method for class 'exdqlmLDVB'
plot(x, type = c("quantile", "component", "state"), index = NULL, ...)
```

Arguments

x	An exdqlmLDVB object.
type	Character string specifying "quantile", "component", or "state".
index	Required for type = "component" or type = "state".
...	Additional arguments.

Examples

```

data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLTVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               dqlm.ind = TRUE, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)

plot(M0)
options(old)

```

plot.exdqlmMCMC

Plot Method for exdqlmMCMC Objects

Description

Plot Method for exdqlmMCMC Objects

Usage

```

## S3 method for class 'exdqlmMCMC'
plot(x, type = c("quantile", "component", "state"), index = NULL, ...)

```

Arguments

x	An exdqlmMCMC object.
type	Character string specifying "quantile", "component", or "state".
index	Required for type = "component" or type = "state".
...	Additional arguments.

Examples

```

data("scIVTmag", package = "exdqlm")
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M2 = exdqlmMCMC(y, p0=0.85, model, df = c(0.98), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.burn = 20, n.mcmc = 20,
               init.from.vb = FALSE, verbose = FALSE)

plot(M2)

```

plot.exdqlmSynthesis *Plot Method for exdqlmSynthesis Objects*

Description

Plot the pointwise posterior predictive interval produced by [quantileSynthesis](#). The method is intentionally separate from `quantileSynthesis()` so the synthesis step remains a computation, while the returned object still has a standard plotting interface.

Usage

```
## S3 method for class 'exdqlmSynthesis'
plot(
  x,
  y = NULL,
  time = NULL,
  add = FALSE,
  interval = 0.95,
  show.median = TRUE,
  show.mean = FALSE,
  band.col = grDevices::adjustcolor("lightblue", alpha.f = 0.35),
  median.col = "blue",
  mean.col = "darkblue",
  y.col = "dark grey",
  border = NA,
  xlab = "time",
  ylab = "posterior predictive synthesis",
  main = NULL,
  xlim = NULL,
  ylim = NULL,
  ...
)
```

Arguments

<code>x</code>	An <code>exdqlmSynthesis</code> object.
<code>y</code>	Optional observed series to overlay.
<code>time</code>	Optional time vector for the synthesized summaries. If omitted, <code>seq_len(T)</code> is used, where <code>T</code> is the number of synthesized time points.
<code>add</code>	Logical; add the synthesis interval to an existing plot.
<code>interval</code>	Numeric in $(0, 1)$ giving the plotted central interval. Currently <code>0.50</code> and <code>0.95</code> are supported from stored summaries.
<code>show.median</code>	Logical; draw the synthesized posterior median.
<code>show.mean</code>	Logical; draw the synthesized posterior mean.
<code>band.col</code>	Fill color for the predictive interval.

median.col	Color for the posterior median line.
mean.col	Color for the posterior mean line.
y.col	Color for the optional observed series.
border	Border color for the predictive interval polygon.
xlab, ylab, main	Graphical labels.
xlim, ylim	Optional axis limits.
...	Additional graphical arguments passed to the initial plot() call when add = FALSE.

polytrendMod	<i>Create an n-th order polynomial exDQLM component</i>
--------------	--

Description

The function creates an n -th order polynomial exDQLM component.

Usage

```
polytrendMod(order, m0, C0, backend = c("auto", "R", "cpp"))
```

Arguments

order	Numeric order n of the polynomial model.
m0	Optional numeric prior mean. Defaults to $n \times 1$ vector of zeros.
C0	Optional numeric prior covariance. Defaults to matrix $10^3 I_n$.
backend	Backend selection for matrix construction: "auto" (default), "R", or "cpp".

Value

An object of class "exdqlm" containing the following:

- FF - $n \times 1$ observational vector.
- GG - $n \times n$ evolution matrix.
- m0 - $n \times 1$ prior mean of the state vector.
- C0 - $n \times n$ prior covariance matrix of the state vector.

Examples

```
# create a second order polynomial component
trend.comp = polytrendMod(2, rep(0, 2), 10*diag(2))
```

predict.exdqlmFit *Forecast Method for Dynamic exdqlmFit Objects*

Description

Computes filtered and k-step-ahead forecast quantiles from a fitted dynamic quantile model. The returned exdqlmForecast object can be printed, summarized, plotted with plot(), or passed to [diagnostics](#).

Usage

```
## S3 method for class 'exdqlmFit'
predict(
  object,
  start.t,
  k,
  fFF = NULL,
  fGG = NULL,
  plot = FALSE,
  add = FALSE,
  cols = c("purple", "magenta"),
  cr.percent = 0.95,
  return.draws = FALSE,
  n.samp = NULL,
  seed = NULL,
  ...
)
```

Arguments

object	A fitted dynamic exdqlmFit object.
start.t	Integer index at which forecasts start.
k	Integer number of steps ahead to forecast.
fFF	Optional state vector(s) for the forecast steps. A numeric matrix with q rows and either 1 column (non–time-varying) or k columns (time-varying). Its dimension must match the fitted model in object.
fGG	Optional evolution matrix/matrices for the forecast steps. Either a numeric $q \times q$ matrix (non–time-varying) or a $q \times q \times k$ array (time-varying). Its dimensions must match the fitted model in object.
plot	Logical; if TRUE, immediately plot the returned forecast object as a convenience shortcut. Default is FALSE.
add	Logical value indicating whether to add the forecasted quantiles to the current plot. Default is FALSE.
cols	Optional character vector of length 2 giving the colors for filtered and forecasted quantiles respectively. Default c("purple", "magenta").

cr.percent	Optional numeric in $(0, 1)$ indicating the probability mass for the credible intervals (e.g., 0.95). Default 0.95.
return.draws	Optional logical; if TRUE, the function also returns a matrix of posterior predictive forecast draws in samp.fore. Default is FALSE.
n.samp	Optional positive integer specifying how many forecast draws to return when return.draws = TRUE. If omitted, all available posterior (σ, γ) draws from object are used.
seed	Optional integer random seed used only for forecast-draw generation when return.draws = TRUE. If provided, the previous R RNG state is restored on exit.
...	Additional arguments (unused).

Value

An object of class "exdqlmForecast" containing the following:

- start.t Integer index at which forecasts start (within the span of the fitted model in object).
- k Integer number of steps ahead forecasted.
- m1 The fitted dynamic model object used to initialize the forecast.
- cr.percent The probability mass for the credible intervals (e.g., 0.95).
- fa Forecast state mean vectors ($q \times k$ matrix).
- fR Forecast state covariance matrices ($q \times q \times k$ array).
- ff Forecast quantile means (length-k numeric).
- fQ Forecast quantile variances (length-k numeric).
- samp.fore Optional posterior predictive forecast draws ($k \times n.samp$) returned when return.draws = TRUE.

Examples

```
# Toy example
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 20L)
y = scIVTmag[1:100]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
  dqlm.ind = TRUE, sig.init = 15, n.samp = 30,
  verbose = FALSE)
M0.forecast = predict(M0, start.t = 90, k = 10,
  return.draws = TRUE, n.samp = 50, seed = 123)
M0.forecast
plot(M0.forecast)
dim(M0.forecast$samp.fore)
options(old)
```

```
print.exalStaticDiagnostic
```

Print Method for exalStaticDiagnostic Objects

Description

Print Method for exalStaticDiagnostic Objects

Usage

```
## S3 method for class 'exalStaticDiagnostic'  
print(x, ...)
```

Arguments

x	An exalStaticDiagnostic object.
...	Additional arguments (unused).

```
print.exalStaticFit
```

Print Method for exalStaticFit Objects

Description

Print Method for exalStaticFit Objects

Usage

```
## S3 method for class 'exalStaticFit'  
print(x, ...)
```

Arguments

x	A fitted static exalStaticFit object.
...	Additional arguments (unused).

print.exalStaticLDVB *Print Method for exalStaticLDVB Objects*

Description

Print Method for exalStaticLDVB Objects

Usage

```
## S3 method for class 'exalStaticLDVB'  
print(x, ...)
```

Arguments

x	An exalStaticLDVB object.
...	Additional arguments (unused).

print.exalStaticMCMC *Print Method for exalStaticMCMC Objects*

Description

Print Method for exalStaticMCMC Objects

Usage

```
## S3 method for class 'exalStaticMCMC'  
print(x, ...)
```

Arguments

x	An exalStaticMCMC object.
...	Additional arguments (unused).

print.exdqlm	<i>Print exDQLM model details</i>
--------------	-----------------------------------

Description

Print the details of the exDQLM model.

Usage

```
## S3 method for class 'exdqlm'
print(x, ...)
```

Arguments

x	a exdqlm object.
...	further arguments (unused).

print.exdqlmDiagnostic	<i>Print Method for exdqlmDiagnostic Objects</i>
------------------------	--

Description

Print Method for exdqlmDiagnostic Objects

Usage

```
## S3 method for class 'exdqlmDiagnostic'
print(x, ...)
```

Arguments

x	An exdqlmDiagnostic object.
...	Additional arguments (unused).

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.95), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
M0.diags = diagnostics(M0)
print(M0.diags)
```

```
options(old)
```

print.exdqlmFit	<i>Print Method for exdqlmFit Objects</i>
-----------------	---

Description

Print Method for exdqlmFit Objects

Usage

```
## S3 method for class 'exdqlmFit'  
print(x, ...)
```

Arguments

x	A fitted dynamic exdqlmFit object.
...	Additional arguments (unused).

print.exdqlmForecast	<i>Print Method for exdqlmForecast Objects</i>
----------------------	--

Description

Print Method for exdqlmForecast Objects

Usage

```
## S3 method for class 'exdqlmForecast'  
print(x, ...)
```

Arguments

x	An exdqlmForecast object.
...	Additional arguments (unused).

Examples

```

data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLTVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               dqlm.ind = TRUE, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
M0.forecast = predict(M0, start.t = 50, k = 5)
print(M0.forecast)
options(old)

```

```
print.exdqlmForecastDiagnostic
```

Print Method for exdqlmForecastDiagnostic Objects

Description

Print Method for exdqlmForecastDiagnostic Objects

Usage

```
## S3 method for class 'exdqlmForecastDiagnostic'
print(x, ...)
```

Arguments

x	An exdqlmForecastDiagnostic object.
...	Additional arguments (unused).

```
print.exdqlmISVB
```

Print Method for exdqlmISVB Objects

Description

Print Method for exdqlmISVB Objects

Usage

```
## S3 method for class 'exdqlmISVB'
print(x, ...)
```

Arguments

x An exdqlmISVB object.
 ... Additional arguments (unused).

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
# Legacy ISVB object retained for backward-compatible inspection methods
M0 = exdqlmISVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.IS = 20, n.samp = 20, tol = 0.2,
               verbose = FALSE)

print(M0)
options(old)
```

print.exdqlmLDVB

Print Method for exdqlmLDVB Objects

Description

Print Method for exdqlmLDVB Objects

Usage

```
## S3 method for class 'exdqlmLDVB'
print(x, ...)
```

Arguments

x An exdqlmLDVB object.
 ... Additional arguments (unused).

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               dqlm.ind = TRUE, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)

print(M0)
options(old)
```

```
print.exdqlmMCMC
```

Print Method for exdqlmMCMC Objects

Description

Print Method for exdqlmMCMC Objects

Usage

```
## S3 method for class 'exdqlmMCMC'
print(x, ...)
```

Arguments

`x` An exdqlmMCMC object.
`...` Additional arguments (unused).

Examples

```
data("scIVTmag", package = "exdqlm")
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M2 = exdqlmMCMC(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.burn = 20, n.mcmc = 20,
               init.from.vb = FALSE, verbose = FALSE)

print(M2)
```

```
print.exdqlmSynthesis
```

Print Method for exdqlmSynthesis Objects

Description

Print Method for exdqlmSynthesis Objects

Usage

```
## S3 method for class 'exdqlmSynthesis'
print(x, ...)
```

Arguments

`x` An exdqlmSynthesis object.
`...` Additional arguments (unused).

qexal

*Quantile Function for the exAL Distribution***Description**

Vectorized over p.

Usage

```
qexal(
  p,
  p0 = 0.5,
  mu = 0,
  sigma = 1,
  gamma = 0,
  lower.tail = TRUE,
  log.p = FALSE
)
```

Arguments

p	Numeric vector of probabilities in (0, 1).
p0	Probability level used in the quantile parametrization. Scalar in (0, 1). Default 0.5.
mu	Location parameter (scalar). Default 0.
sigma	Scale parameter (scalar, strictly positive). Default 1.
gamma	Skewness parameter controlling asymmetry (scalar). Must be within valid bounds implied by p0. Default 0.
lower.tail	Logical scalar; if TRUE (default) return $P(X \leq q)$, otherwise $P(X > q)$.
log.p	Logical scalar; if TRUE, return log-probabilities.

Value

Numeric vector of quantiles (same length as p).

Examples

```
p <- seq(0.1, 0.9, by = 0.2)
q <- qexal(p, p0 = 0.5, mu = 0, sigma = 1, gamma = 0)
all.equal(p, pexal(q, p0 = 0.5, mu = 0, sigma = 1, gamma = 0), tol = 1e-4)
```

quantileSynthesis	<i>Synthesize a unified posterior predictive distribution from multiple quantile-model draws</i>
-------------------	--

Description

The function synthesizes posterior predictive draws from multiple fitted quantile models into a single posterior predictive distribution. It uses a two-step correction: (i) isotonic regression at the grid of target quantiles to align the fitted quantile levels, and (ii) distributional alignment (shift each model's draws so its tau-quantile matches the isotone anchor). It then builds a single predictive quantile function per time by piecewise-linear blending across adjacent quantile models with optional global monotone rearrangement.

Usage

```
quantileSynthesis(
  draws_list,
  p,
  enforce_isotonic = TRUE,
  rearrange = TRUE,
  grid_M = 1001L,
  n_samp = 1000L,
  seed = NULL,
  T_expected = NULL
)
```

Arguments

<code>draws_list</code>	List of length <code>L</code> ; each element is either: (i) a numeric matrix of posterior predictive draws ($T \times ns$ or $ns \times T$), (ii) a fitted dynamic <code>exdqlmFit</code> object such as an <code>exdqlmMCMC</code> , <code>exdqlmLDVB</code> , or legacy <code>exdqlmISVB</code> fit with <code>samp.post.pred</code> , or (iii) an <code>exdqlmForecast</code> object with <code>samp.fore</code> . Rows are coerced to time.
<code>p</code>	Numeric vector of target quantile levels in $(0,1)$ of length <code>L</code> (same order as <code>draws_list</code> , not necessarily sorted). Duplicate levels are not allowed.
<code>enforce_isotonic</code>	Logical; apply isotonic regression (PAVA) over the grid <code>p</code> at each time <code>t</code> to remove crossing. Default <code>TRUE</code> .
<code>rearrange</code>	Logical; apply monotone rearrangement (evaluate $\rightarrow$ sort $\rightarrow$ reinterpolate) on a dense grid over <code>u</code> in $(0,1)$. Default <code>TRUE</code> .
<code>grid_M</code>	Integer; size of dense grid <code>M</code> for rearrangement ($u_k = k/(M+1)$). Default <code>1001L</code> .
<code>n_samp</code>	Integer; number of synthesized draws per time. Default <code>1000L</code> .
<code>seed</code>	<code>NULL</code> or integer for reproducible synthesized draws. Default <code>NULL</code> .
<code>T_expected</code>	Optional integer; if provided, forces the time dimension to <code>T_expected</code> when orienting each matrix to $T \times ns$. This avoids accidental transposes.

Value

An object of class "exdqlmSynthesis", which is a list containing:

- draws - Numeric matrix $T \times n_{\text{samp}}$ of synthesized draws.
- levels - Sorted copy of p (length L).
- quantiles - Numeric matrix $T \times L$ of isotone anchors $m^*_{i,t}$.
- summary - List with row-wise summaries of draws (mean, q025, q250, q500, q750, q975).
- method - List of synthesis settings used (name, isotonic, rearrange, grid_M, T_{inferred}).

Examples

```
# short example
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 10L)
TT = 50
y = scIVTmag[1:TT]

# create a compact trend model
trend.comp = polytrendMod(1, stats::quantile(y, 0.85), 10)
model = trend.comp

# fit quantiles using LDVB and save posterior predictive samples
fits <- draws <- NULL
p0s = c(0.10, 0.50, 0.90)
for(i in 1:length(p0s)){
  fits[[i]] = exdqlmLDVB(
    y, p0 = p0s[i], model, df = 0.98, dim.df = 1,
    sig.init = 15, n.samp = 20, tol = 0.2, verbose = FALSE
  )
  draws[[i]] = fits[[i]]$samp.post.pred
}

# synthesize posterior predictive from all quantiles
syn = quantileSynthesis(
  draws_list = draws,
  p = p0s,
  T_expected = TT)

# alternatively, pass fitted dynamic objects directly
syn2 = quantileSynthesis(
  draws_list = fits,
  p = p0s,
  T_expected = TT)

# plot the synthesized 95% posterior predictive interval
plot(syn2, y = y)
options(old)
```

regMod

*Create a standard regression component for an exDQLM***Description**

The function constructs a regression block where the observation vector at time t is $F_t = X_t$ (row of the design matrix), and the state evolves as $\theta_t = \theta_{t-1}$ (i.e., $G_t = I_n$).

Usage

```
regMod(X, m0, C0)
```

Arguments

<code>X</code>	A numeric matrix of dimension $T \times n$ (T time points, n regressors). Vectors are accepted and treated as $T \times 1$.
<code>m0</code>	Optional numeric prior mean (length n). Defaults to zeros.
<code>C0</code>	Optional numeric prior covariance ($n \times n$). Defaults to $10^3 I_n$.

Details

Input X is a $T \times n$ matrix of regressors; the returned FF is an $n \times T$ matrix (i.e., $t(X)$), consistent with component composition via `+.exdqlm`.

Value

An object of class "exdqlm" with elements:

- FF - $n \times T$ matrix with column t equal to $F_t = X_t$.
- GG - $n \times n$ identity matrix (static coefficients).
- m0, C0 - Prior mean/covariance for regression coefficients.

Examples

```
data("climateIndices", package = "exdqlm")

T <- 150
bt_dates <- seq(as.Date("1987-01-01"), by = "month", length.out = T)
idx <- match(bt_dates, climateIndices$date)
X <- scale(climateIndices[idx, c("noi", "amo")])

# Single regressor (T x 1)
reg1 = regMod(X[, "noi"])
# Multiple regressors (T x n)
reg2 = regMod(X)

# Combine with trend/seasonal components
trend.comp = polytrendMod(order = 3, m0 = rep(0,3), C0 = diag(3))
```

```

seas.comp = seasMod(p = 12, h = 1, C0 = diag(1, 2))
base.mod  = trend.comp + seas.comp
model.std = base.mod + reg2

```

rexal

Random Sample Generation for the exAL Distribution

Description

Random Sample Generation for the exAL Distribution

Usage

```
rexal(n, p0 = 0.5, mu = 0, sigma = 1, gamma = 0)
```

Arguments

n	Positive integer number of samples to draw (scalar).
p0	Probability level used in the quantile parametrization. Scalar in (0, 1). Default 0.5.
mu	Location parameter (scalar). Default 0.
sigma	Scale parameter (scalar, strictly positive). Default 1.
gamma	Skewness parameter controlling asymmetry (scalar). Must be within valid bounds implied by p0. Default 0.

Value

Numeric vector of length n.

Examples

```

set.seed(1)
rexal(3, p0 = 0.5, mu = c(-1, 0, 1))

```

scIVTmag

Time series of daily average magnitude IVT in Santa Cruz, CA.

Description

ECMWF Re-Analysis 5 (ERA5) daily average magnitude IVT in Santa Cruz, CA (approximately 22 N, 122 W) from January 1, 1979 to December 31, 2019 with all February 29ths omitted.

Usage

```
scIVTmag
```

Format

A time series of length 14965.

Source

<https://cds.climate.copernicus.eu>

References

Hersbach, H, Bell, B, Berrisford, P, et al. *The ERA5 global reanalysis*. Q J R Meteorol Soc. 2020; 146: 1999– 2049. doi:10.1002/qj.3803

seasMod

Create Fourier representation of a periodic exDQLM component

Description

The function creates a Fourier form periodic component for given period and harmonics.

Usage

```
seasMod(p, h, m0, C0, backend = c("auto", "R", "cpp"))
```

Arguments

p	Numeric period.
h	Numeric vector of harmonics to be included.
m0	Optional numeric prior mean. Defaults to $q \times 1$ vector of zeros where q is the dimension of the period component.
C0	Optional numeric prior covariance. Defaults to matrix $10^3 I_q$.
backend	Backend selection for matrix construction: "auto" (default), "R", or "cpp".

Value

An object of class "exdqlm" containing the following:

- FF - $q \times 1$ observational vector.
- GG - $q \times q$ evolution matrix.
- m0 - $q \times 1$ prior mean of the state vector.
- C0 - $q \times q$ prior covariance matrix of the state vector.

Examples

```
# create a seasonal component with first, second and fourth harmonics of a period of 365
seas.comp = seasMod(365, c(1, 2, 4), C0 = 10*diag(6))
```

```
summary.exalStaticDiagnostic
```

Summary Method for exalStaticDiagnostic Objects

Description

Summary Method for exalStaticDiagnostic Objects

Usage

```
## S3 method for class 'exalStaticDiagnostic'
summary(object, ...)
```

Arguments

object	An exalStaticDiagnostic object.
...	Additional arguments (unused).

```
summary.exalStaticFit
```

Summary Method for exalStaticFit Objects

Description

Prints a compact summary of a fitted static AL/exAL quantile-regression model and returns the displayed summary tables for programmatic inspection.

Usage

```
## S3 method for class 'exalStaticFit'
summary(object, max.coef = 6L, ...)
```

Arguments

object	A fitted static exalStaticFit object.
max.coef	Maximum number of coefficients to print in the coefficient summary table.
...	Additional arguments (unused).

Value

Invisibly returns a list with data frames describing stored draws, scalar posterior summaries, and coefficient summaries.

`summary.exalStaticLDVB`*Summary Method for exalStaticLDVB Objects*

Description

Summary Method for exalStaticLDVB Objects

Usage

```
## S3 method for class 'exalStaticLDVB'  
summary(object, ...)
```

Arguments

object	An exalStaticLDVB object.
...	Additional arguments (unused).

`summary.exalStaticMCMC`*Summary Method for exalStaticMCMC Objects*

Description

Summary Method for exalStaticMCMC Objects

Usage

```
## S3 method for class 'exalStaticMCMC'  
summary(object, ...)
```

Arguments

object	An exalStaticMCMC object.
...	Additional arguments (unused).

summary.exdqlm	<i>Summary exDQLM model details</i>
----------------	-------------------------------------

Description

Print the details of the exDQLM model.

Usage

```
## S3 method for class 'exdqlm'
summary(object, ...)
```

Arguments

object	a exdqlm object.
...	further arguments (unused).

summary.exdqlmDiagnostic	<i>Summary Method for exdqlmDiagnostic Objects</i>
--------------------------	--

Description

Summary Method for exdqlmDiagnostic Objects

Usage

```
## S3 method for class 'exdqlmDiagnostic'
summary(object, ...)
```

Arguments

object	An exdqlmDiagnostic object.
...	Additional arguments (unused).

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.95), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
M0.diags = diagnostics(M0)
summary(M0.diags)
```

options(old)

summary.exdqlmFit	<i>Summary Method for exdqlmFit Objects</i>
-------------------	---

Description

Prints a compact summary of a fitted dynamic quantile state-space model and returns the displayed summary tables for programmatic inspection.

Usage

```
## S3 method for class 'exdqlmFit'
summary(object, ...)
```

Arguments

object	A fitted dynamic exdqlmFit object.
...	Additional arguments (unused).

Value

Invisibly returns a list with data frames describing stored draws, scalar posterior summaries, and convergence information.

summary.exdqlmForecast	<i>Summary Method for exdqlmForecast Objects</i>
------------------------	--

Description

Summary Method for exdqlmForecast Objects

Usage

```
## S3 method for class 'exdqlmForecast'
summary(object, ...)
```

Arguments

object	An exdqlmForecast object.
...	Additional arguments (unused).

Examples

```

data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLTVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               dqlm.ind = TRUE, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)
M0.forecast = predict(M0, start.t = 50, k = 5)
summary(M0.forecast)
options(old)

```

summary.exdqlmForecastDiagnostic

Summary Method for exdqlmForecastDiagnostic Objects

Description

Summary Method for exdqlmForecastDiagnostic Objects

Usage

```

## S3 method for class 'exdqlmForecastDiagnostic'
summary(object, ...)

```

Arguments

object	An exdqlmForecastDiagnostic object.
...	Additional arguments (unused).

summary.exdqlmISVB

Summary Method for exdqlmISVB Objects

Description

Summary Method for exdqlmISVB Objects

Usage

```

## S3 method for class 'exdqlmISVB'
summary(object, ...)

```

Arguments

object	An exdqlmISVB object.
...	Additional arguments (unused).

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
# Legacy ISVB object retained for backward-compatible inspection methods
M0 = exdqlmISVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.IS = 20, n.samp = 20, tol = 0.2,
               verbose = FALSE)

summary(M0)
options(old)
```

summary.exdqlmLDVB	<i>Summary Method for exdqlmLDVB Objects</i>
--------------------	--

Description

Summary Method for exdqlmLDVB Objects

Usage

```
## S3 method for class 'exdqlmLDVB'
summary(object, ...)
```

Arguments

object	An exdqlmLDVB object.
...	Additional arguments (unused).

Examples

```
data("scIVTmag", package = "exdqlm")
old = options(exdqlm.max_iter = 15L)
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M0 = exdqlmLDVB(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               dqlm.ind = TRUE, sig.init = 15,
               n.samp = 20, tol = 0.2, verbose = FALSE)

summary(M0)
options(old)
```

summary.exdqlmMCMC	<i>Summary Method for exdqlmMCMC Objects</i>
--------------------	--

Description

Summary Method for exdqlmMCMC Objects

Usage

```
## S3 method for class 'exdqlmMCMC'
summary(object, ...)
```

Arguments

object	An exdqlmMCMC object.
...	Additional arguments (unused).

Examples

```
data("scIVTmag", package = "exdqlm")
y = scIVTmag[1:60]
model = polytrendMod(1, stats::quantile(y, 0.85), 10)
M2 = exdqlmMCMC(y, p0 = 0.85, model, df = c(0.98), dim.df = c(1),
               gam.init = -3.5, sig.init = 15,
               n.burn = 20, n.mcmc = 20,
               init.from.vb = FALSE, verbose = FALSE)
summary(M2)
```

summary.exdqlmSynthesis	<i>Summary Method for exdqlmSynthesis Objects</i>
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Description

Summary Method for exdqlmSynthesis Objects

Usage

```
## S3 method for class 'exdqlmSynthesis'
summary(object, time = NULL, ...)
```

Arguments

<code>object</code>	An <code>exdqlmSynthesis</code> object.
<code>time</code>	Optional vector of time values. If supplied, it must have length equal to the number of rows in <code>object\$draws</code> .
<code>...</code>	Additional arguments (unused).

Value

A data frame containing pointwise summaries of the synthesized posterior predictive draws.

Index

- * **datasets**
 - BTflow, 8
 - climateIndices, 9
 - ELIanos, 19
 - scIVTmag, 98
- * **package**
 - exdqlm-package, 4
- + .exdqlm, 7
- as.exdqlm, 8
- BTflow, 8
- climateIndices, 9
- compPlot, 10
- compPlot(), 4
- dexal, 11
- diagnostics, 12, 39, 84
- diagnostics(), 4, 6
- diagnostics.exalStaticFit, 13
- diagnostics.exdqlmFit, 14
- diagnostics.exdqlmForecast, 17
- ELIanos, 19
- exal_make_mcmc_control, 30
- exal_make_mcmc_control(), 27, 50
- exal_make_mcmc_dqlm_sigma_control, 31
- exal_make_mcmc_dqlm_sigma_control(), 30
- exal_make_mcmc_latent_state_control, 31
- exal_make_mcmc_latent_state_control(), 30
- exal_make_mcmc_sigmagam_control, 32
- exal_make_mcmc_sigmagam_control(), 27, 30
- exal_make_mcmc_theta_control, 33
- exal_make_mcmc_theta_control(), 30
- exal_make_vb_control, 34
- exal_make_vb_control(), 23, 30, 47
- exal_make_vb_sigmagam_control, 35
- exal_make_vb_sigmagam_control(), 34
- exal_make_vb_sts_control, 36
- exal_make_vb_sts_control(), 34
- exalStaticDiagnostics, 19
- exalStaticLDVB, 20, 21, 74
- exalStaticLDVB(), 4, 34, 35
- exalStaticMCMC, 20, 25, 74
- exalStaticMCMC(), 4, 30, 32, 35
- exdqlm (exdqlm-package), 4
- exdqlm-package, 4
- exdqlmDiagnostics, 20, 37
- exdqlmDiagnostics(), 6, 18, 41, 42
- exdqlmForecast, 17, 39
- exdqlmForecast(), 4, 41
- exdqlmForecastDiagnostics, 41
- exdqlmISVB, 10, 37, 43, 53
- exdqlmISVB(), 4, 40
- exdqlmLDVB, 10, 37, 46, 53, 60
- exdqlmLDVB(), 4, 34–36, 40, 43
- exdqlmMCMC, 10, 37, 49, 53
- exdqlmMCMC(), 4, 30–33, 35, 40
- exdqlmPlot, 53
- exdqlmPlot(), 4
- exdqlmTransferISVB, 55
- exdqlmTransferISVB(), 4
- exdqlmTransferLDVB, 58
- exdqlmTransferLDVB(), 4, 55
- exdqlmTransferMCMC, 62
- exdqlmTransferMCMC(), 4
- get_gamma_bounds, 67
- is.exalStaticDiagnostic, 68
- is.exalStaticFit, 68
- is.exalStaticLDVB, 68
- is.exalStaticMCMC, 69
- is.exdqlm, 69
- is.exdqlmDiagnostic, 69
- is.exdqlmFit, 70

is.exdqlmForecast, 70
is.exdqlmForecastDiagnostic, 70
is.exdqlmISVB, 71
is.exdqlmLDVB, 71
is.exdqlmMCMC, 71
is.exdqlmSynthesis, 72

pexal, 72
plot, 74–76
plot(), 4
plot.exalStaticDiagnostic, 14, 20, 73
plot.exalStaticFit, 74
plot.exalStaticLDVB, 75
plot.exalStaticMCMC, 75
plot.exdqlmDiagnostic, 76
plot.exdqlmFit, 77
plot.exdqlmForecast, 79
plot.exdqlmISVB, 79
plot.exdqlmLDVB, 80
plot.exdqlmMCMC, 81
plot.exdqlmSynthesis, 82
polytrendMod, 83
polytrendMod(), 4
predict(), 4
predict.exdqlmFit, 17, 84
print.exalStaticDiagnostic, 86
print.exalStaticFit, 86
print.exalStaticLDVB, 87
print.exalStaticMCMC, 87
print.exdqlm, 88
print.exdqlmDiagnostic, 88
print.exdqlmFit, 89
print.exdqlmForecast, 89
print.exdqlmForecastDiagnostic, 90
print.exdqlmISVB, 90
print.exdqlmLDVB, 91
print.exdqlmMCMC, 92
print.exdqlmSynthesis, 92

qexal, 93
quantileSynthesis, 72, 82, 94
quantileSynthesis(), 4

regMod, 96
regMod(), 4
rexal, 97

scIVTmag, 98
seasMod, 98

seasMod(), 4
summary.exalStaticDiagnostic, 99
summary.exalStaticFit, 99
summary.exalStaticLDVB, 100
summary.exalStaticMCMC, 100
summary.exdqlm, 101
summary.exdqlmDiagnostic, 101
summary.exdqlmFit, 102
summary.exdqlmForecast, 102
summary.exdqlmForecastDiagnostic, 103
summary.exdqlmISVB, 103
summary.exdqlmLDVB, 104
summary.exdqlmMCMC, 105
summary.exdqlmSynthesis, 105